

Robust estimate of the dark matter halo of the Milky-way's dwarf spheroidal galaxies

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In collaboration with
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arXiv:1701.xxxxx

arXiv:1608.01749 (submitted in MNRAS)

MNRAS, 461, 2914 (1603.08046 [astro-ph.GA])

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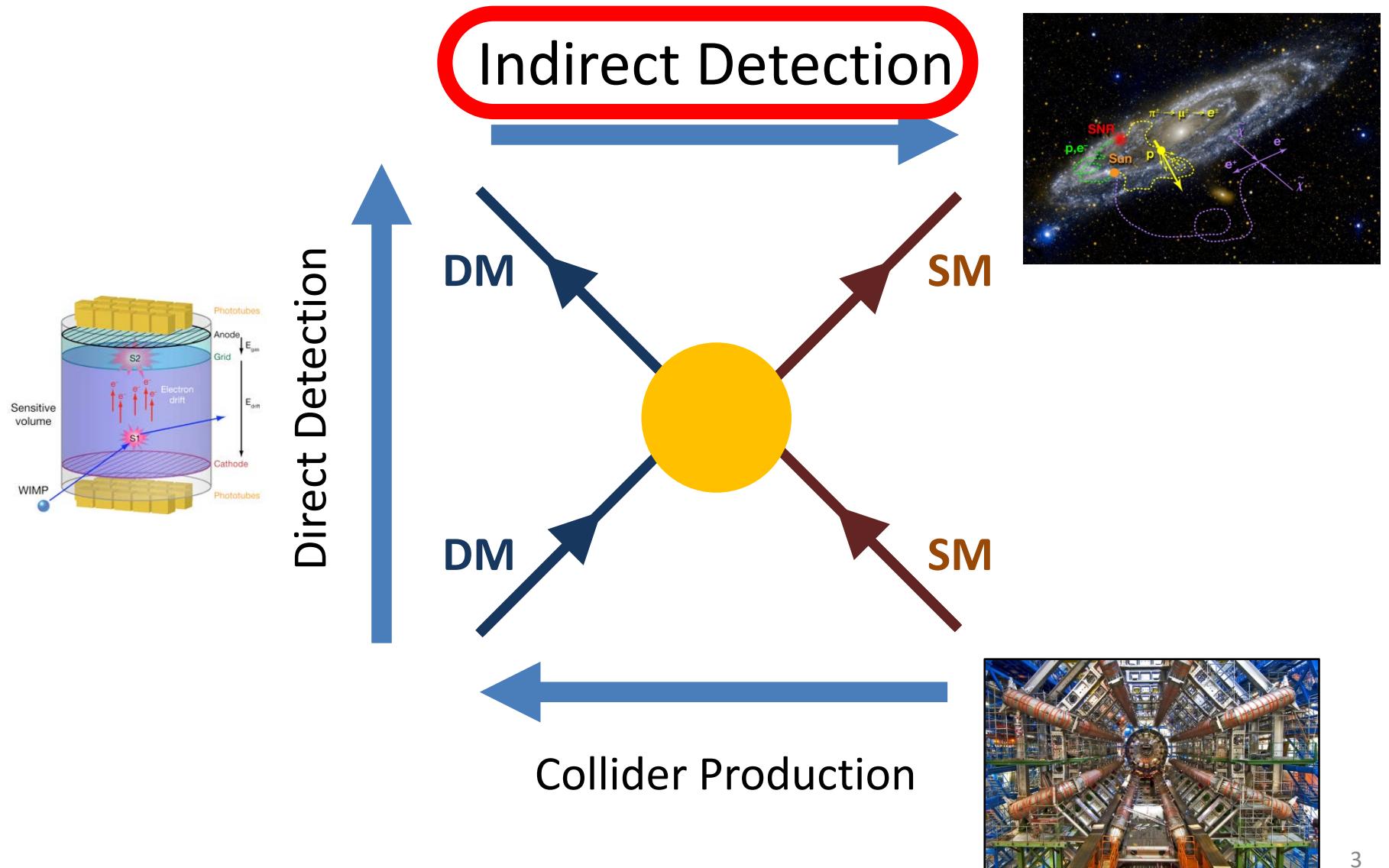
from model

from fit

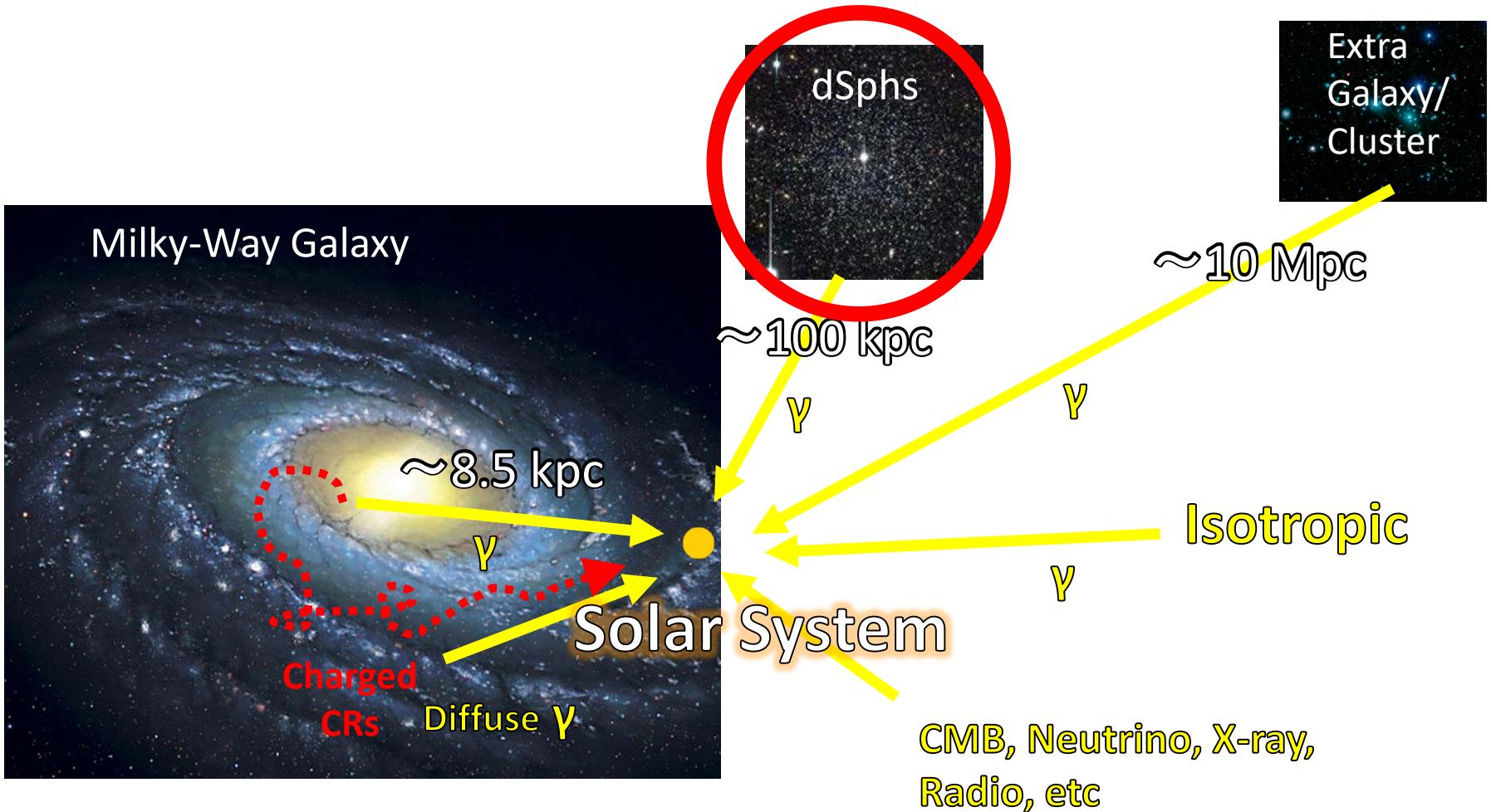
from data

4. Future

Dark Matter Search



Indirect Detection



Dwarf spheroidal galaxies

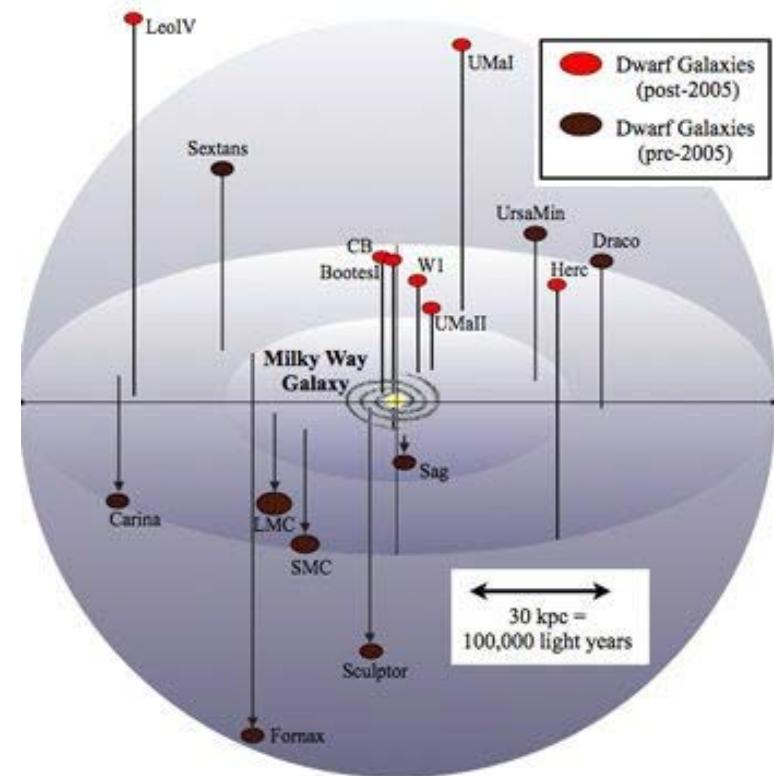
dSphs:

1. **Satellite** galaxies: $d = 10 \sim 100 \text{ kpc}$
2. **Clean** (no strong gamma-ray source)
3. **DM rich**

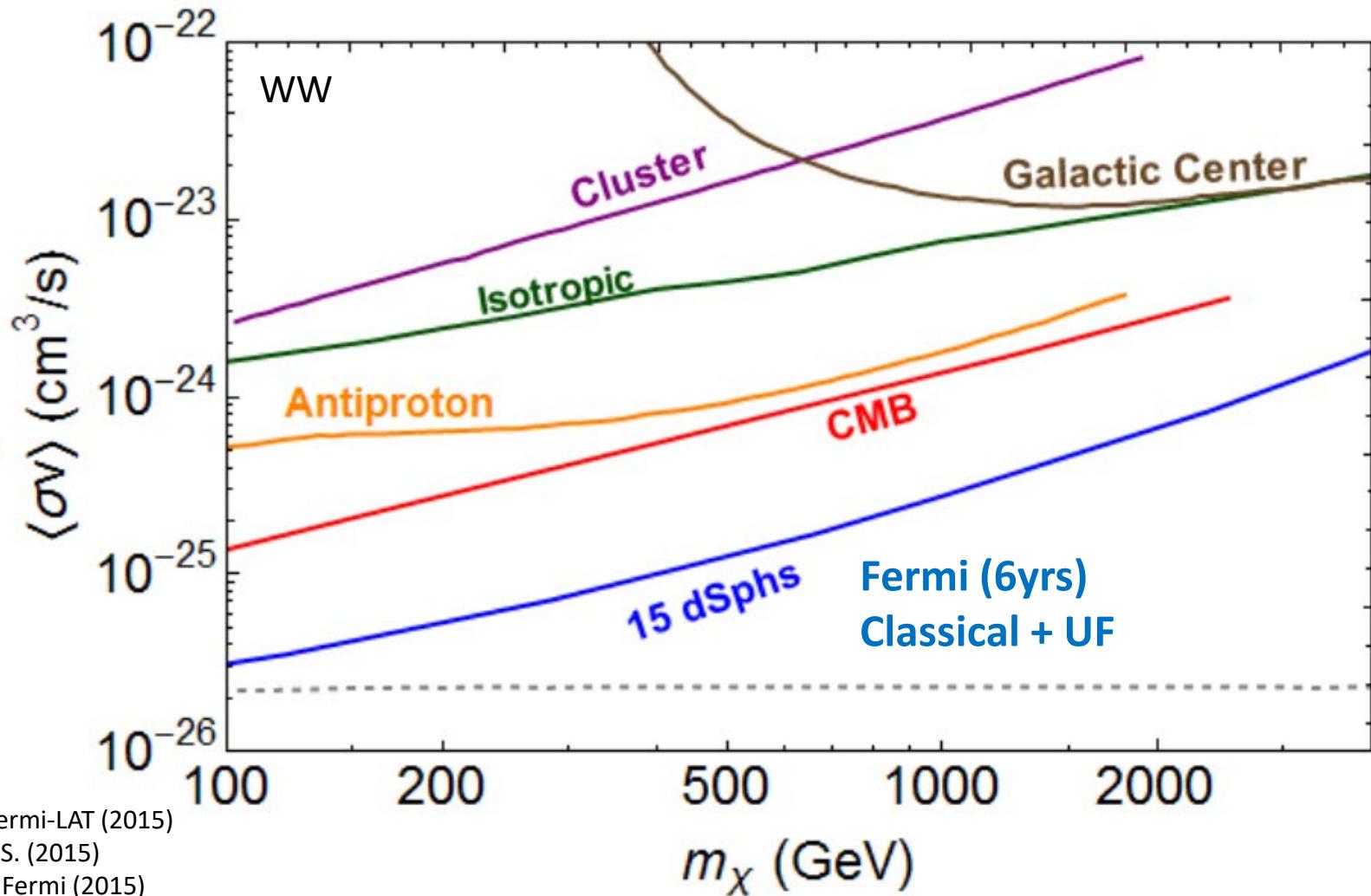
dSph Type

	Classical	Ultra-faint
#dSphs	8	>20
M/L (M_\odot/L_\odot)	10-100	100-1000
Distance (kpc)	60-250	10-60
#Obs Stars	150-2500	20-100
Characteristics	Brighter, farther	Darker, closer

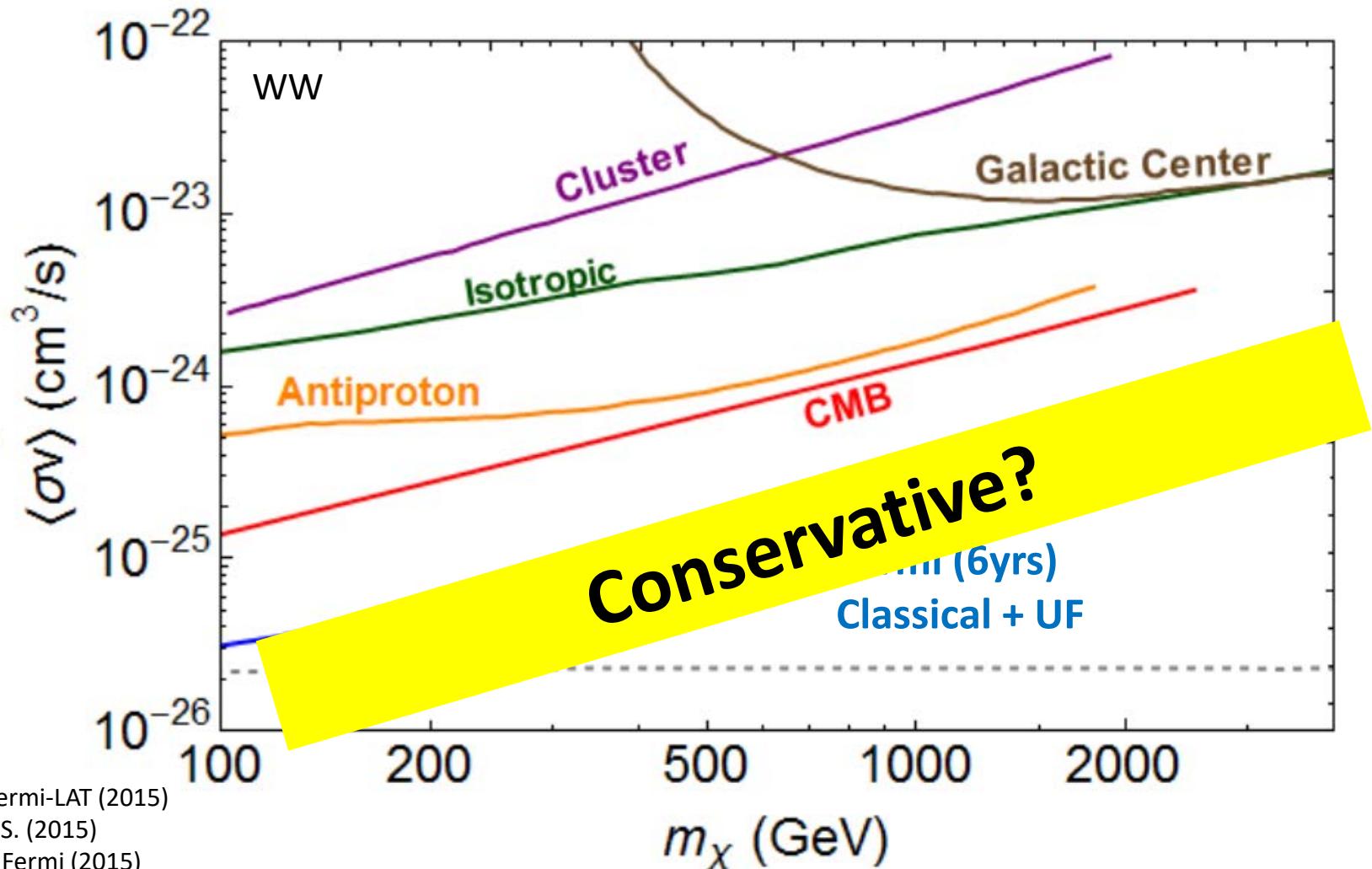
See, e.g. Wolf et al (2010)



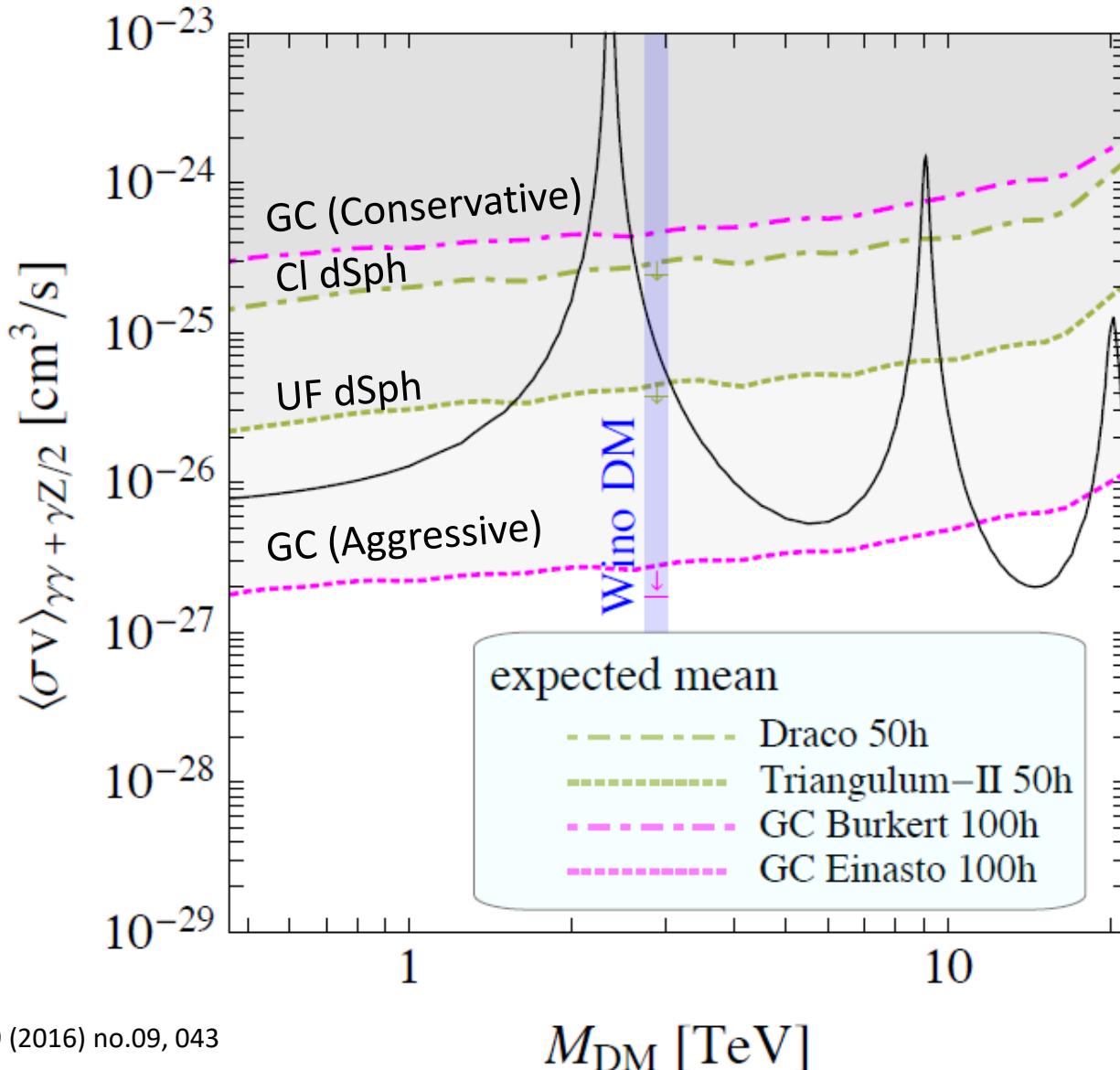
dSph = Strong Probe



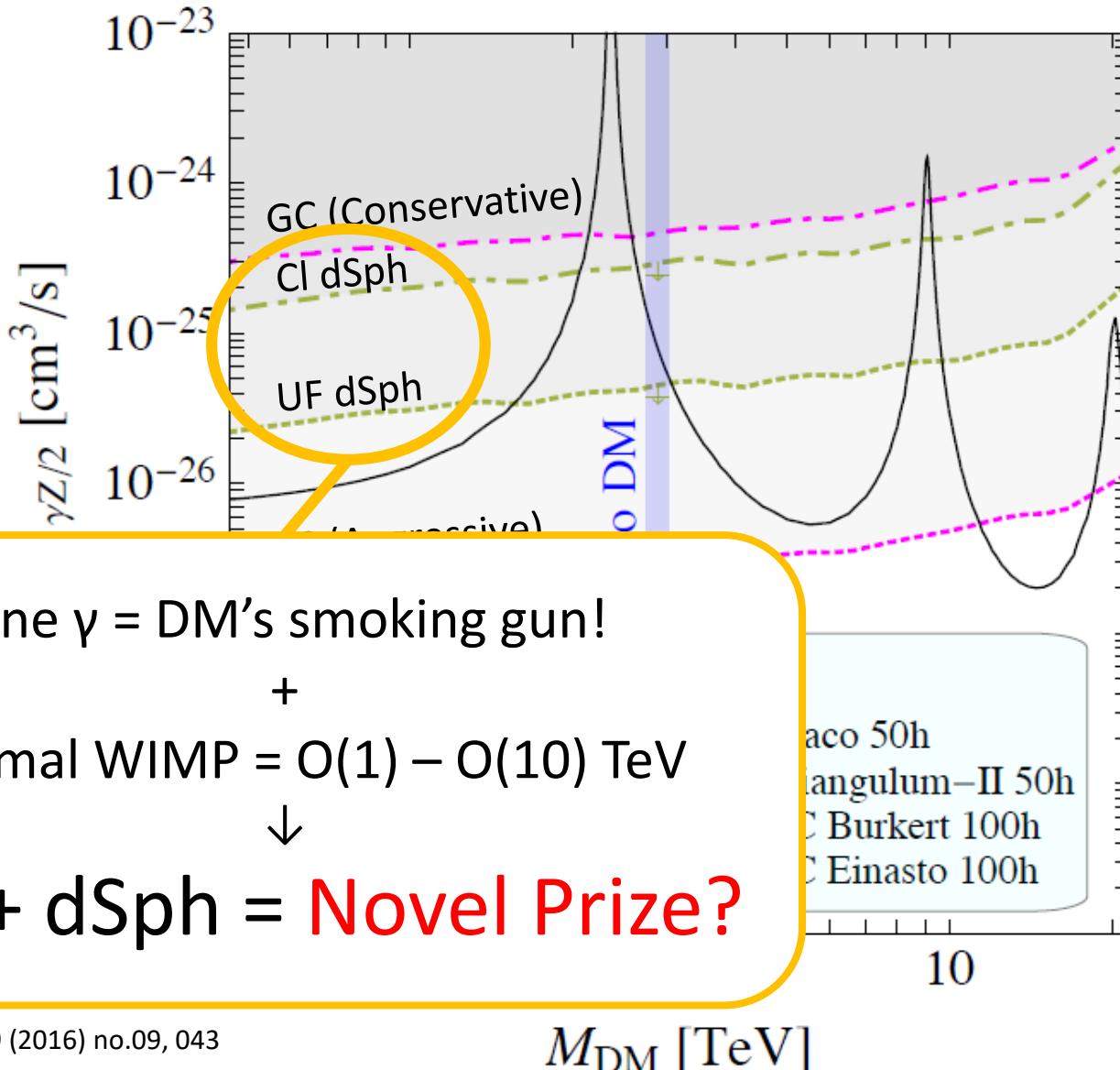
dSph = Strong Probe



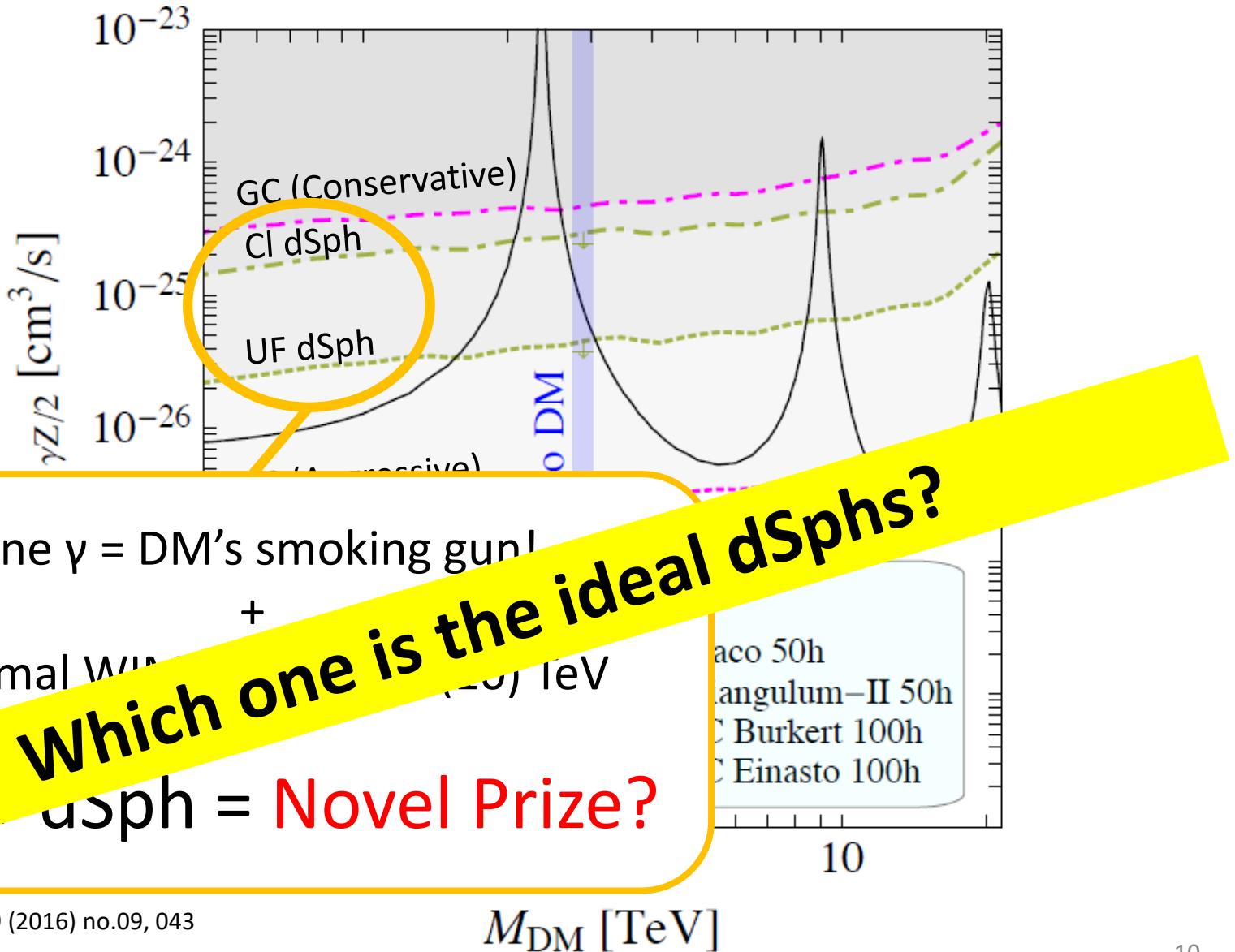
$O(1)$ TeV Line Search = CTA !



$O(1)$ TeV Line Search = CTA !



$O(1)$ TeV Line Search = CTA !



Signal Flux

Dwarf galaxy



$$\frac{\Phi(E, \Delta\Omega)}{\text{Observed } \gamma\text{-Ray Flux}} = \frac{\left[\frac{\langle \sigma v \rangle}{8\pi m_{\text{DM}}^2} \sum_f \text{Br}(\text{DM DM} \rightarrow f) \left(\frac{dN_\gamma}{dE} \right) \right]}{\text{DM Property}} \left[\int_{\Delta\Omega} d\Omega \int_{\text{l.o.s}} dl \rho^2(l, \Omega) \right]$$

Halo Profile
(J-factor)

→ J-factor is determined by

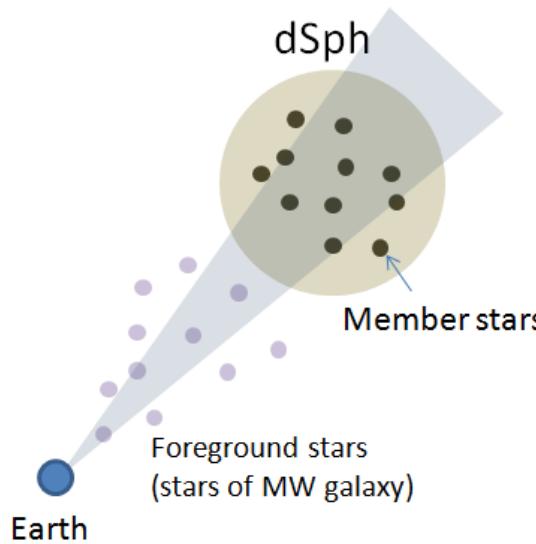
stellar kinematics of dSph

Observables

Distance from center: R_{proj}

Luminosity, Color

⇒ By photometry ($V \sim 26$)



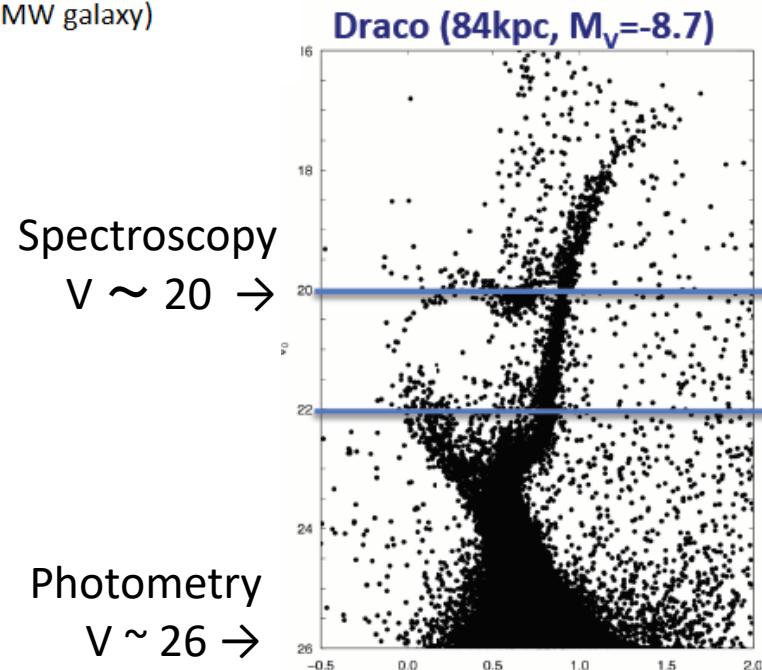
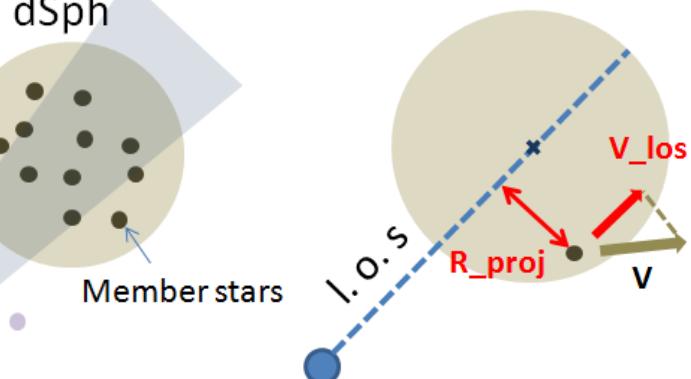
Recession velocity: v_{los}

Metallicity

=> By spectroscopy ($V \sim 20$)

Data set $\{R_{\text{proj}}, v_{\text{los}}\}$ is typically
 $O(100-1000)$ for classical dSphs and
 $< O(50)$ for UF-dSphs

- v_{los} cannot be directly used for fit.
- binned v_{los} data w.r.t. R_{proj} gives a dispersion curve $\sigma(R_{\text{proj}})$.



Dispersion Curve

DM Density profile

$$\rho(r) = \rho_s (r/r_s)^{-\gamma} [1 + (r/r_s)^\alpha]^{(\gamma-\beta)/\alpha}$$

$\rho_s (r/r_s)^{-1} (1+r/r_s)^{-2}$	Cusp
$\rho_s (1+r/r_s)^{-1} (1+r/r_s)^{-2}$	Cored

Stellar Density
Profile: $v(r)$



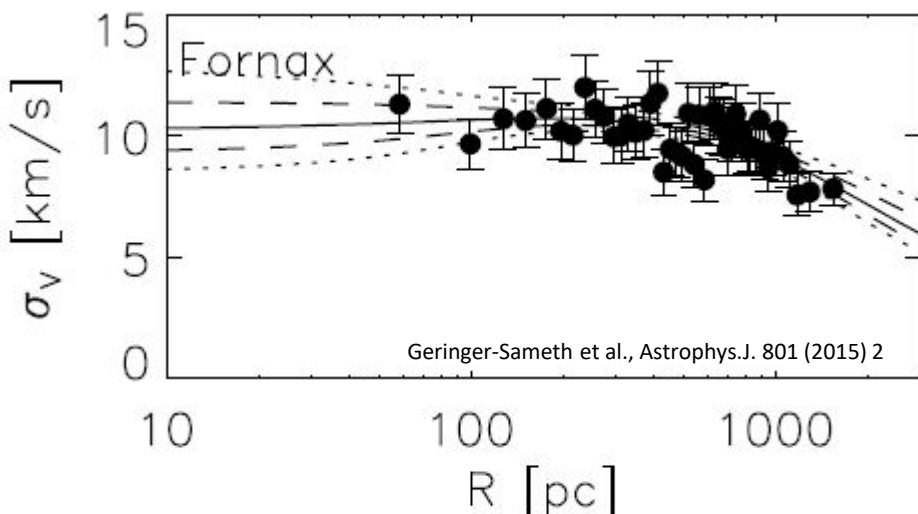
Jeans equation
for stars

$$\frac{1}{\nu} \frac{d}{dr} (\nu v_r^2) + 2 \frac{\beta(r) v_r^2}{r} = - \frac{GM(r)}{r^2}$$

$\sigma_{\text{l.o.s}}^2$ (Theory)

$\sigma_{\text{l.o.s}}^2$ (obs)

Fit



$$P(\theta|D) \propto P(D|\theta)P(\theta)$$

$$\sim \prod_i^{\text{samples}} \exp \left[- \frac{(\sigma_{\text{obs}}^2(r_i) - \sigma_{\text{theory}}^2(r_i, \theta))^2}{2\delta^2} \right]$$

Current Status

Is the fit model accurate enough?

Enough data?

Is the data pure enough?

Current Status

Is the fit model accurate enough?

Spherical
Assumption

Enough data?

$O(10) - O(100)$

Is the data pure enough?

95%

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Non Sphericity

Most of the studies assume
spherical profile.

But...

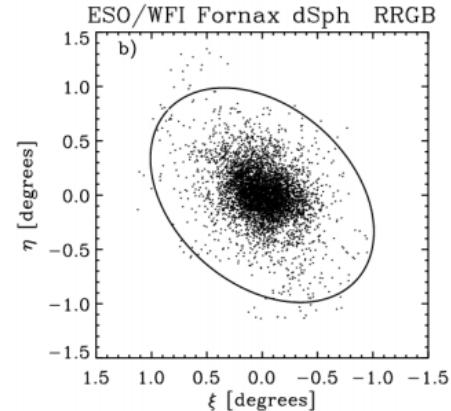
1. Stellar distributions of dSphs are not spherical.
2. Simulation suggest axisymmetric profile.
3. Non-Spherical fit include spherical possibility.

→ non-spherical fit

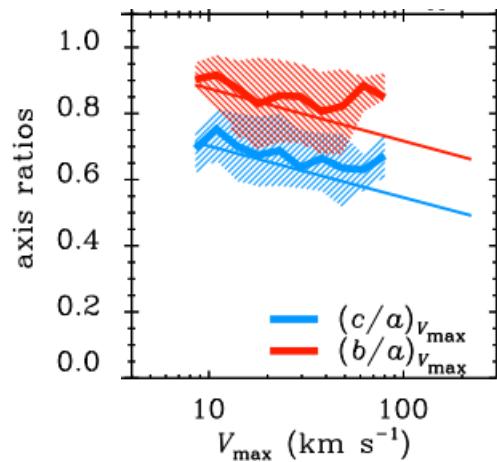
is more conservative

K. Hayashi and M. Chiba 2012, 2015b,

K. Hayashi, KI, S. Matsumoto, M. Ibe, M. N. Ishigaki, H. Sugai, arXiv:1603.08046 [astro-ph.GA]



G. Battaglia et al. Astron.Astrophys.
459



C. Vera-Ciro, et al. MNRAS 439
(2014).

Axisymmetric fit

Assumptions

1. Dynamical equilibrium.
2. DM dominate system.
3. Collisionless system.
4. Axisymmetry in both stellar and DM components.
5. Constant velocity anisotropy.

Parameters

Halo Size ρ_0

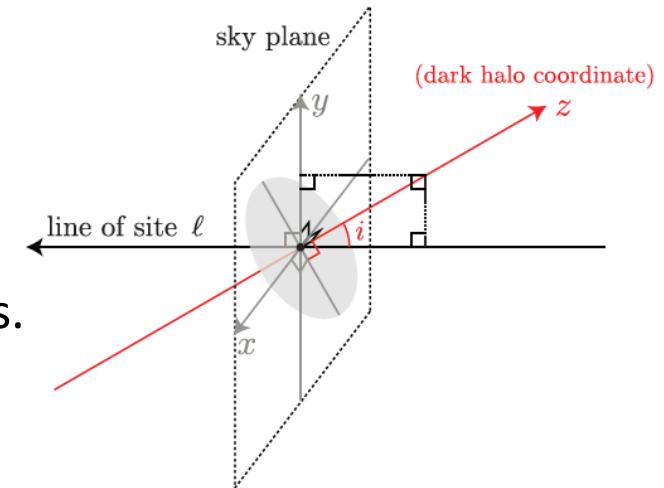
Halo Radius b_{halo}

Halo Shape α

Axis-ratio Q

Inclination i

Velocity anisotropy β_z



$$\rho(R, z) = \rho_0 \left(\frac{m}{b_{\text{halo}}} \right)^\alpha \left[1 + \left(\frac{m}{b_{\text{halo}}} \right)^2 \right]^{-(\alpha+3)/2}$$

$$m^2 = R^2 + \frac{z^2}{Q^2}$$

$$\beta_z = 1 - \overline{v_z^2} / \overline{v_R^2}$$

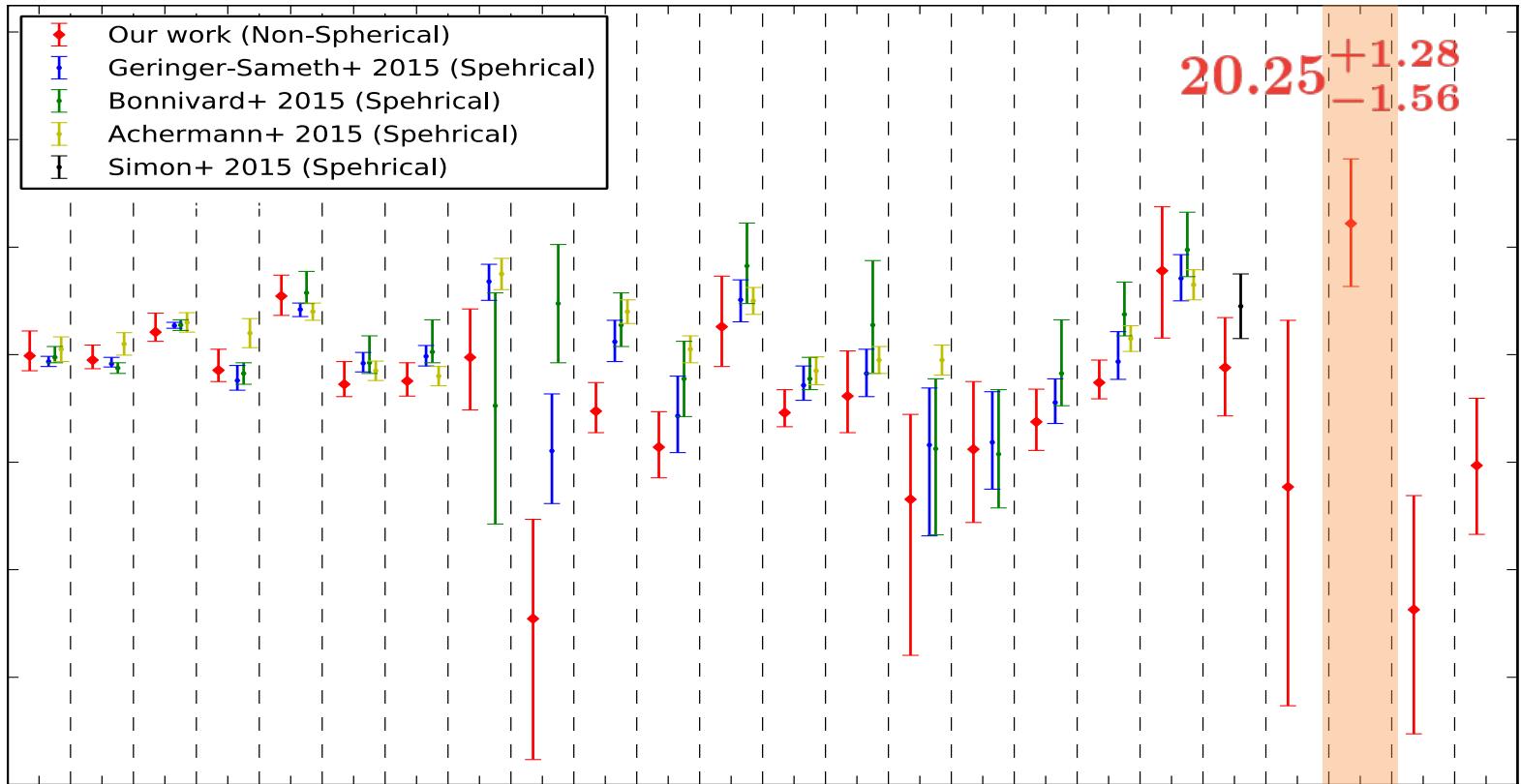
Axisymmetric Jeans equations $\rightarrow \overline{v_{\text{los}}^2}(x, y)$

$$\overline{v_z^2} = \frac{1}{\nu(R, z)} \int_z^\infty \nu \frac{\partial \Phi}{\partial z} dz$$

$$\overline{v_\phi^2} = \frac{1}{1 - \beta_z} \left[\overline{v_z^2} + \frac{R}{\nu} \frac{\partial (\nu \overline{v_z^2})}{\partial R} \right] + R \frac{\partial \Phi}{\partial R}$$

Our Fit Results

$$\mathcal{F} = \int_{\Delta\Omega} \int_{\Omega} \int_{l.o.s} \rho^2(\ell, \Omega)$$

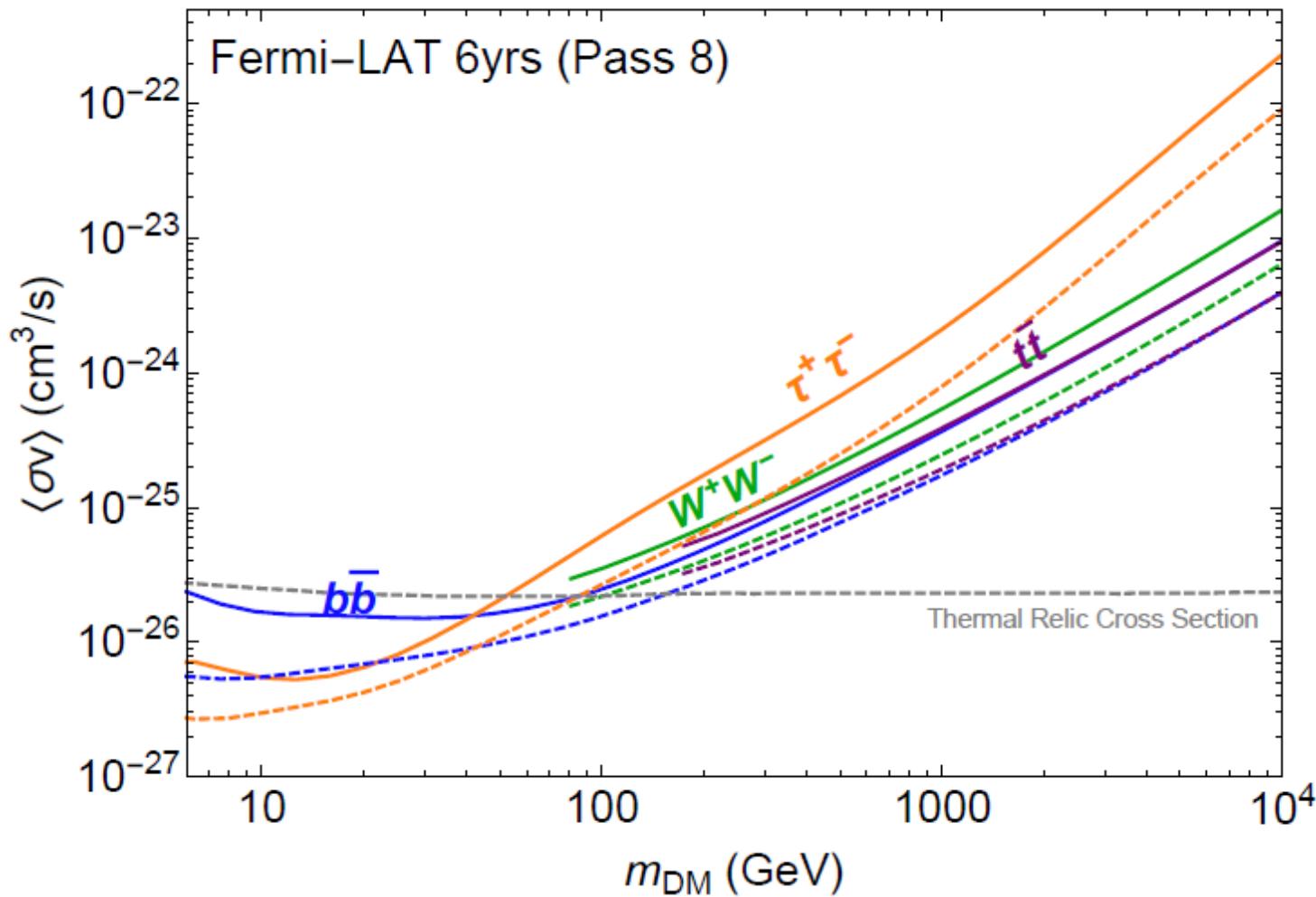


※The fit is still affected by the range of the parameter region.

Empirical condition: $r^* < r_s$ is required for UF dSph
with small J-factors.

- $0 \leq \log_{10}[b_{\text{halo}}/\text{pc}] \leq +5$;
- $-5 \leq \log_{10}[\rho_0/(M_\odot \text{pc}^{-3})] \leq +5$;

Effect on constraints



Our estimation gives 3 times weaker constraints

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Axisymmetric fit

Enough data?

O(10) – O(100)

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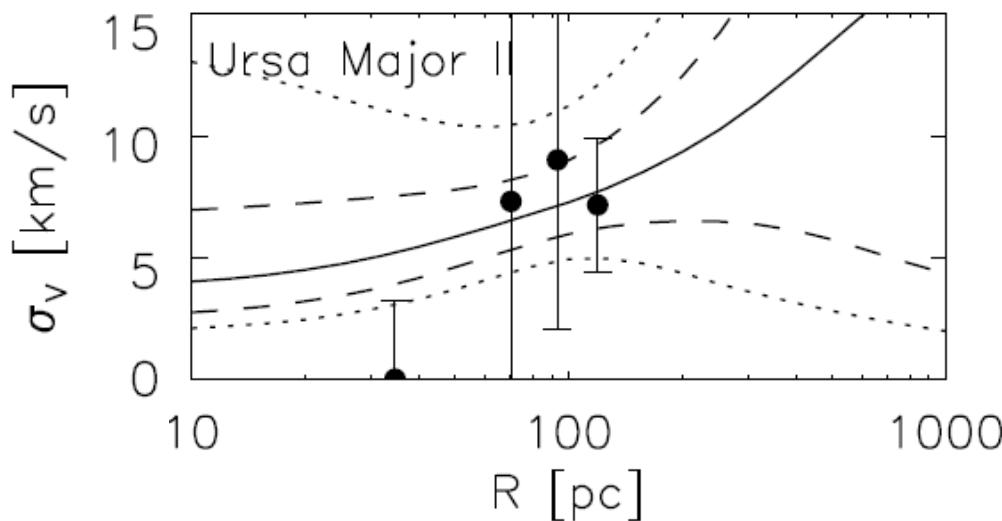
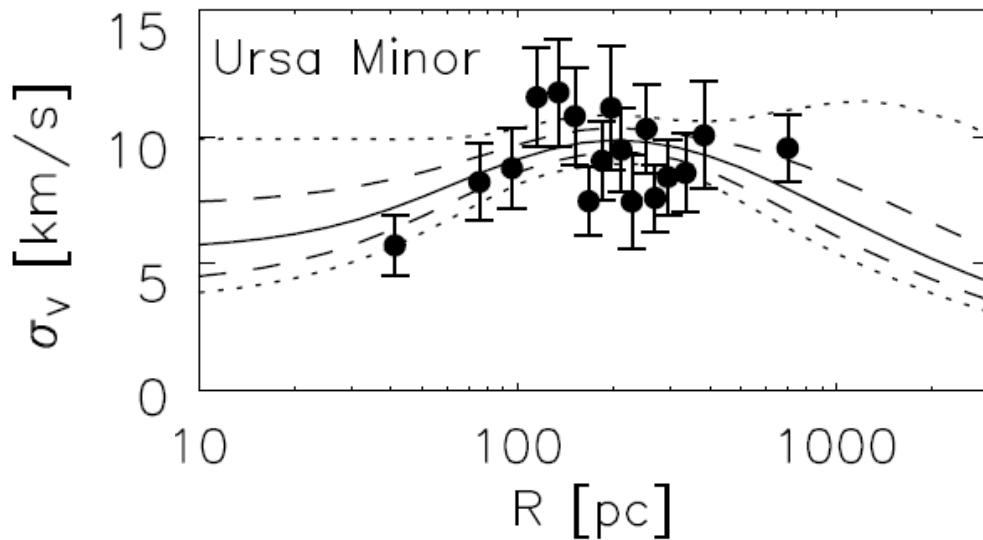


Enough

Is the da

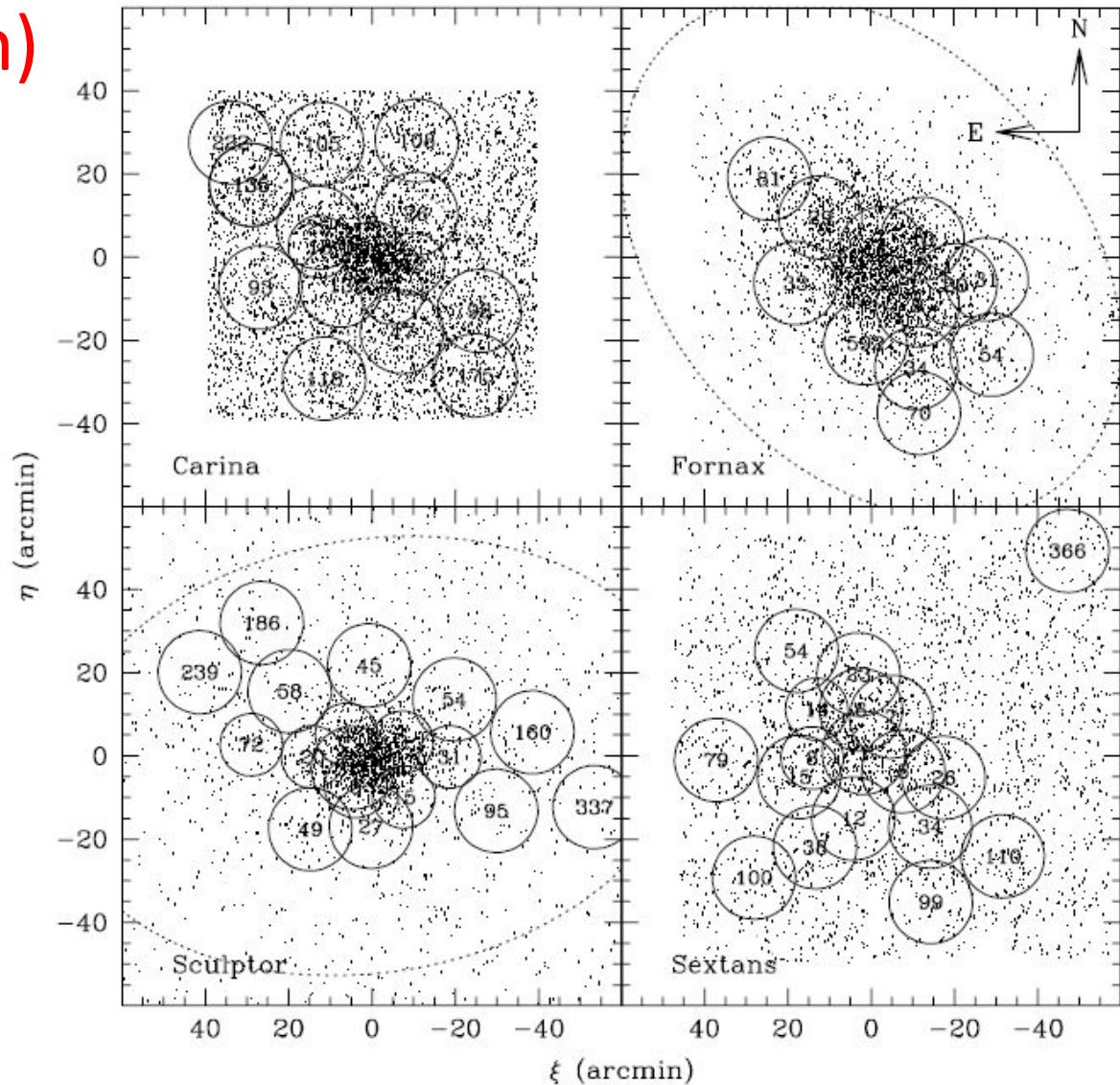
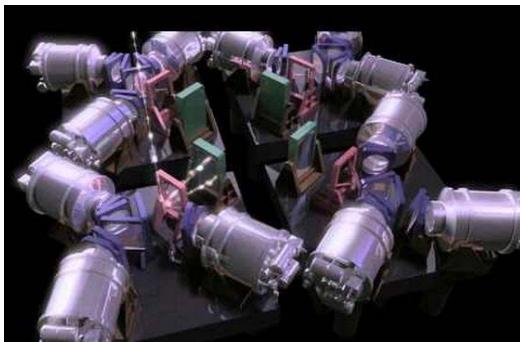
cal
tation

(100)



Prime Focus Spectrograph

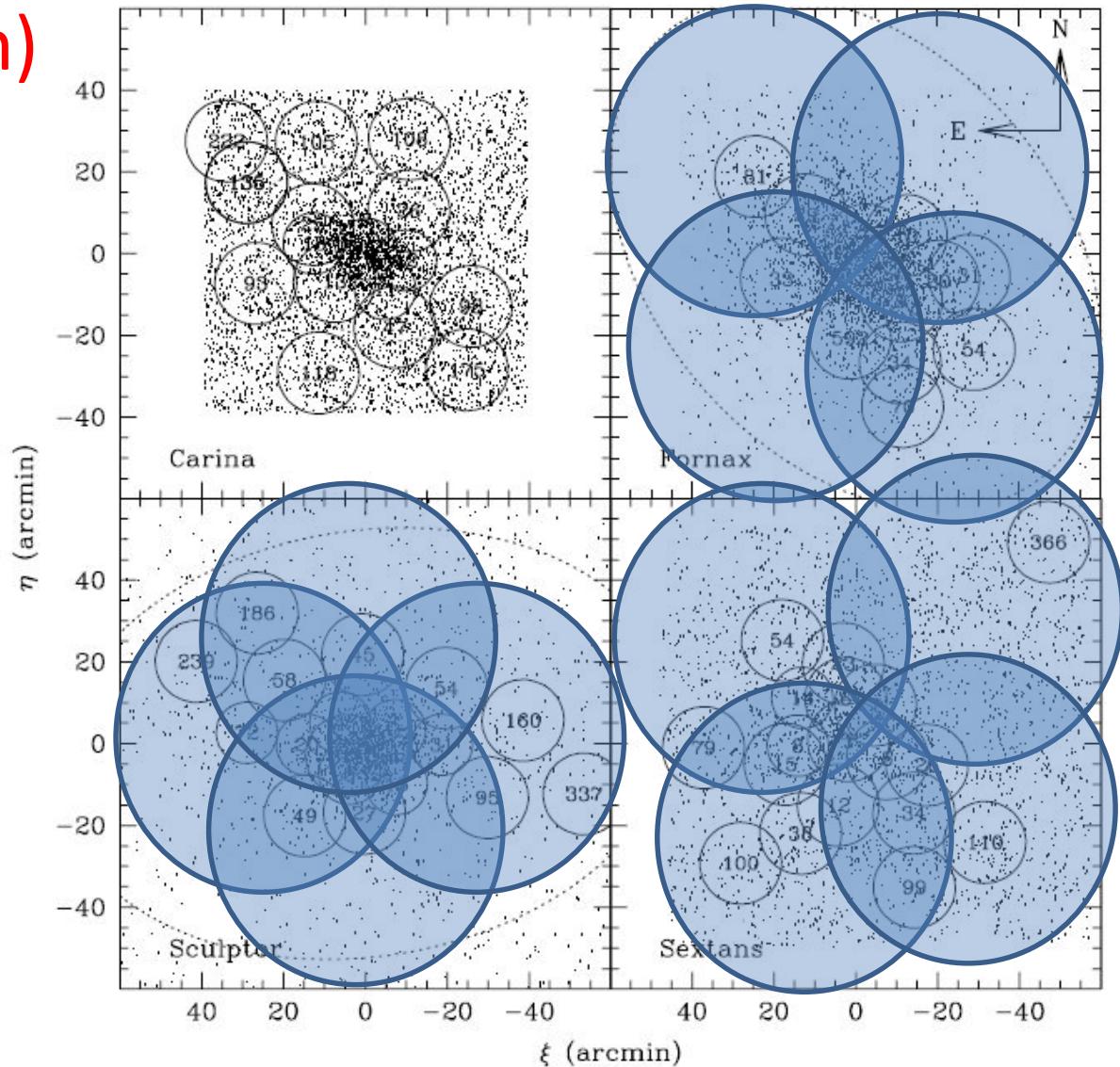
FoV 1.3 deg (diam)
with 2394 Fiber



MMFS (M. G. Walker et al., (2007))

Prime Focus Spectrograph

FoV 1.3 deg (diam)
with 2394 Fiber



MMFS (M. G. Walker et al., (2007))

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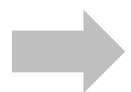
Spherical
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Axisymmetric fit

Enough data?

$O(10) - O(100)$



Increase #data

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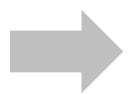
Spherical
Assumption



Axisymmetric fit

Enough data?

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Increase #data

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Hidden Systematics...

Prior Bias?/Cut?

$N < 100$: $> O(1)$ uncertainty

Non Spherical?

$0.2 \sim 0.4$ uncertainty

Velocity anisotropy?

Etc. (Halo truncation, stability, binary stars...)

Foreground Contamination?

$N < 100$: $O(1)$ uncertainty

$N \sim 1000$: < 0.4

In the future...

Increasing
#Obs Star can reduce
these errors

Remains!

Q. How to treat this FG
contamination?

Purpose

- Q.** How many stars will be observed?
- Q.** How can we obtain purer dSph member star data?
- Q.** How can we include the FG contamination in the fit?

Set up

1. Mock Observable: dSph Stellar + Foreground dSph Stellar Mock

⇒ Assign stellar information
(Age, metalicity, luminosity, color, etc)

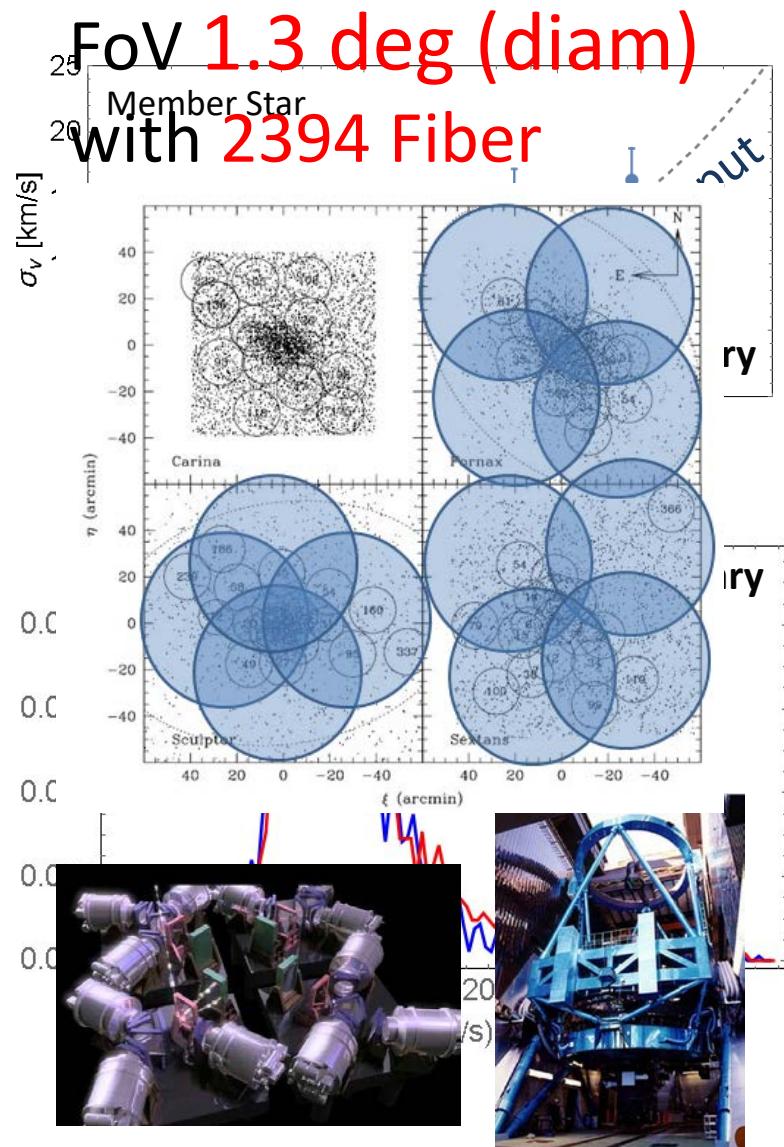
⇒ Assign velocity and distance,
(Boltzmann Equation under DM profile)

Foreground Mock

⇒ Besancon Model (Robin+ (2003))

2. Detector: Prime Focus Spectrograph

θ_{ROI} [degree]	i_{max} [mag]	dv [km/s]	$d[\text{Fe}/\text{H}]$	$d \log_{10}(g/\text{cm/s}^2)$	$d T_{\text{eff}}$ [K]
0.65, 1.3	21, 21.5	3.0	0.5	0.5	500



Cut Strategy

ROI Cut:

0.65 deg radius for 1 pointing

velocity Cut

$v_{Lower} < v < v_{Upper}$

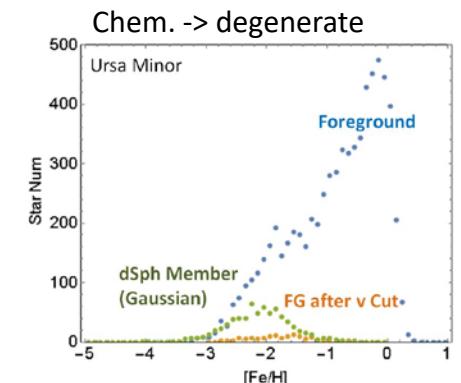
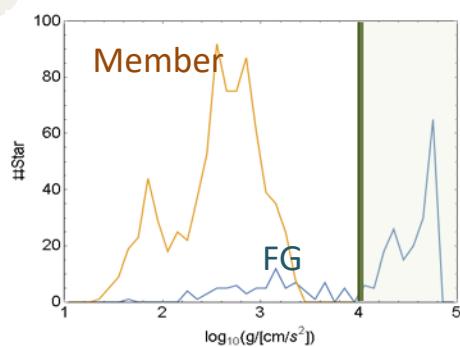
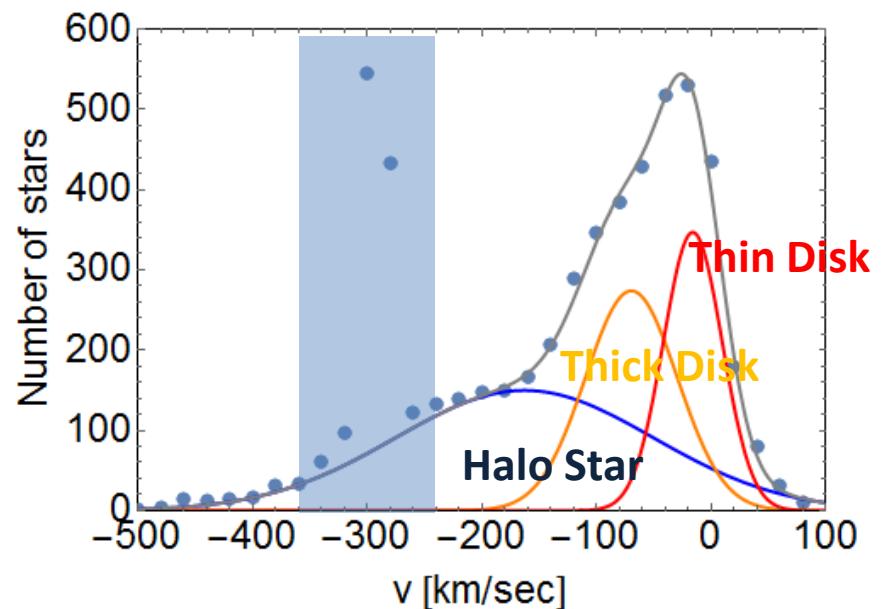
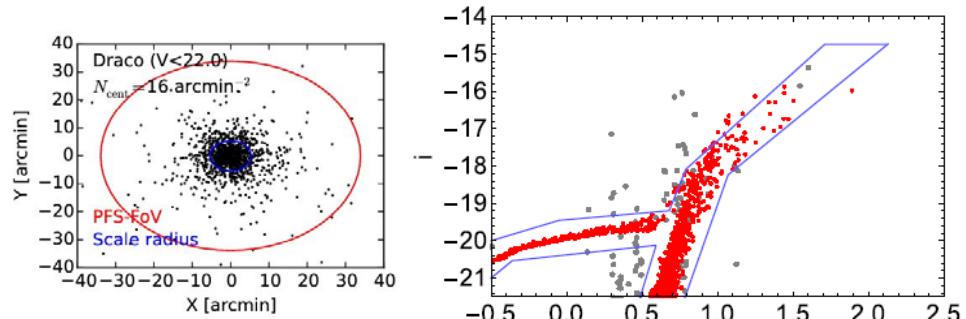
Surface Gravity Cut

$$\propto M/4\pi R^2 \propto MT^4/L \propto (\text{Luminosity})^{-1}$$

Eliminate Darker Foreground Star

Color –Magnitude Cut

* Teff, Chemical Cut do not so efficient



#Obs Expectation

	Current	i > 21	i > 21.5	i > 22
Draco	450	900 37	1150 43	-
Ursa Minor	300	1100 33	1400 41	-
Ursa Major 2	20	50 135	115 180	195 220

Fit including FG model

$$-2 \sum_i \ln(s \underline{f_{\text{Mem}}(v_i, R_i)} + (1 - s) \underline{f_{\text{FG}}(v_i, R_i)})$$

Member Fraction **Prob. Dist. Of FG**

$$s = \frac{N_{\text{Mem}}}{N_{\text{Mem}} + N_{\text{FG}}}$$

$$f_{\text{Mem}}(v, R) = \frac{2\pi R \Sigma(R)}{\sqrt{2\pi \sigma^2(R)}} e^{-\frac{(v - v_{\text{Mem}})^2}{2\sigma^2(R)}}$$
$$f_{\text{FG}}(v, R) = 2\pi R N_{\text{FG}} e^{-\frac{(v - v_{\text{FG}})^2}{2\sigma_{\text{FG}}^2}}$$

Member Parameter
= halo information

FG Parameter

Can be considered to be
Gaussian after several cuts.

Fit Results

Contaminated

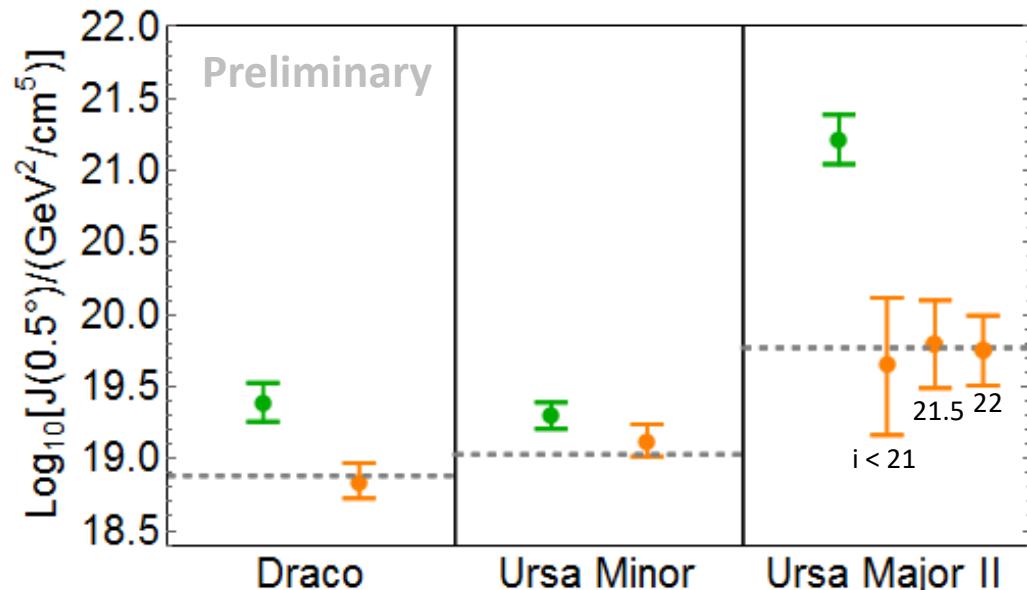
(consider FG as Member star)

5% Contamination biases

$d\log J \approx 0.3 - 0.5$

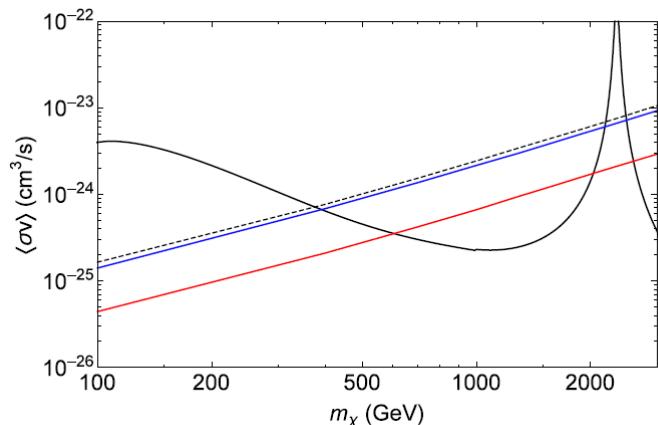
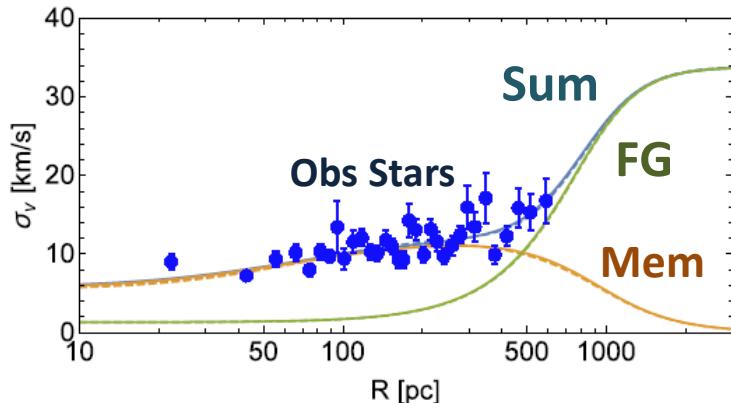
⇒ Overestimates sensitivity line

~ 2-3 times stronger



Our Fit

$$-2 \sum_i \ln(s f_{\text{Mem}}(v_i, R_i) + (1 - s) f_{\text{FG}}(v_i, R_i)) \rightarrow \text{Reproduce Ref val.}$$



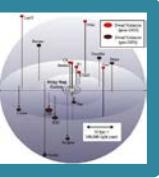
Summary

- Indirect detection is essential for $O(1)$ TeV DM search.
- Gamma-ray observation of dSphs can give robust constraints (~ 1 TeV or More) if $d\log J$ is small enough.
- However, many hidden systematic errors still exist.
- We give more conservative results by the axisymmetric DM model.
- Prior bias gives too aggressive results.
- Investigation of stellar kinematics (PFS) will play a crucial role.
- Reduction of foreground stars can be achieved by our cut and new likelihood.

Thank You !

Koji Ichikawa

In collaboration with
Kohei Hayashi , Masahiro Ibe, Miho N. Ishigaki,
Shigeki Matsumoto and Hajime Sugai.



Kashiwa, Dec. 16, 2016

