

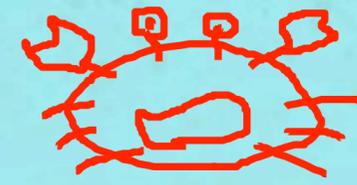
# パルサー星雲における 高エネルギー粒子の空間分布

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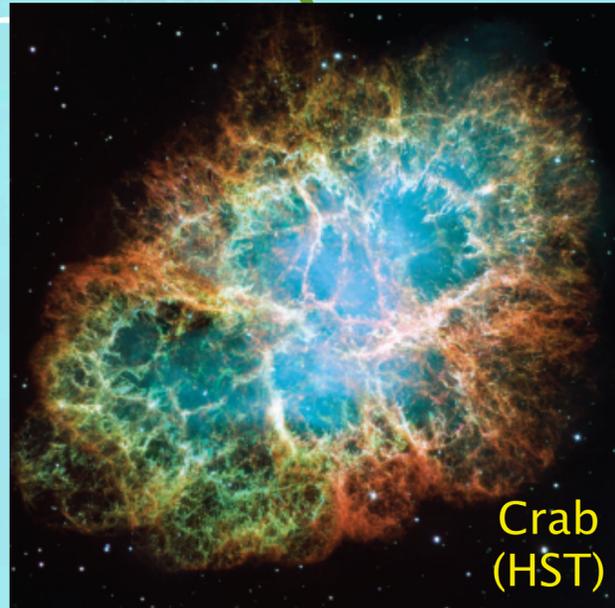
共同研究者: 山崎 了 (青学), 大平 豊 (青学)

3, Sep., 2013, 高エネルギーガンマ線でみる極限宇宙@宇宙線研

# Introduction to



## PWN (Pulsar wind nebula)



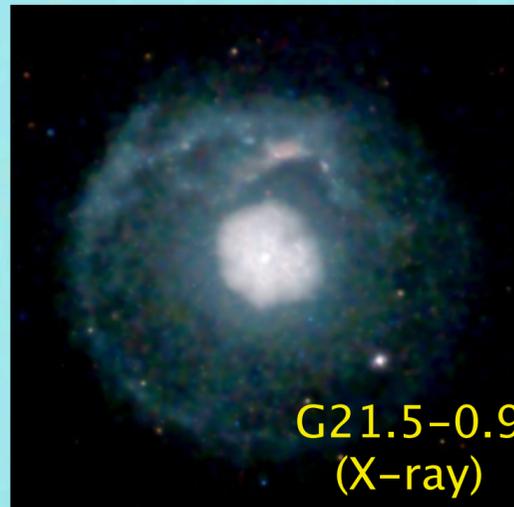
Crab  
(HST)

**Line emission  
(SN ejecta)**



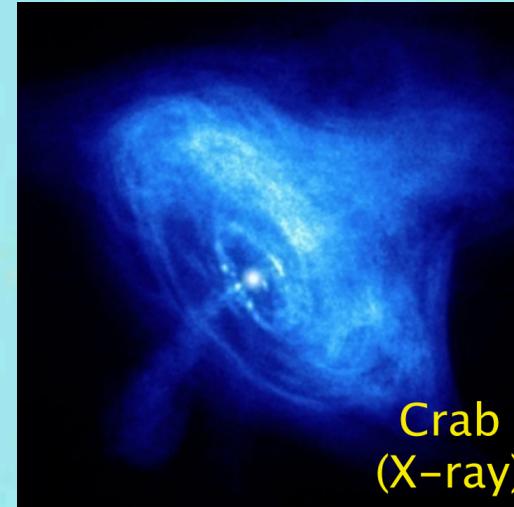
Crab  
(radio - X-ray)

**Non-thermal  
(Pulsar wind)**



G21.5-0.9  
(X-ray)

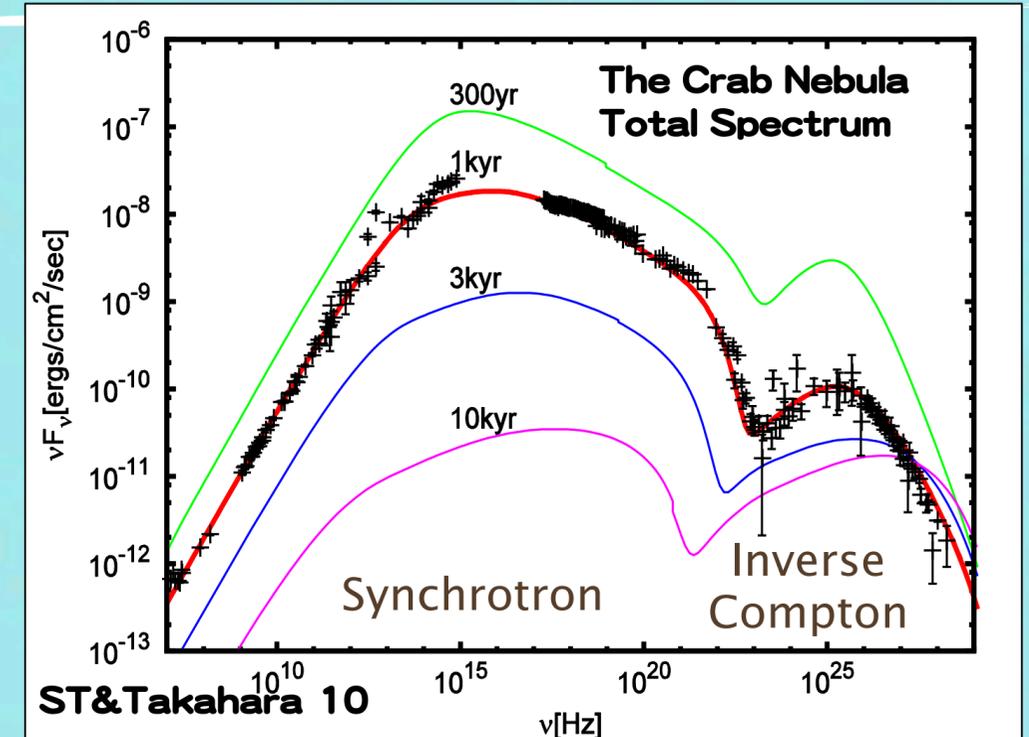
**Confined by SNR**



Crab  
(X-ray)

**Powered by PSR**

## Total spectrum



**We reproduced**

- Total spectrum @ 1kyr
- Flux decrease rate  $\sim 0.2\%$ /year @ radio

**We obtain**

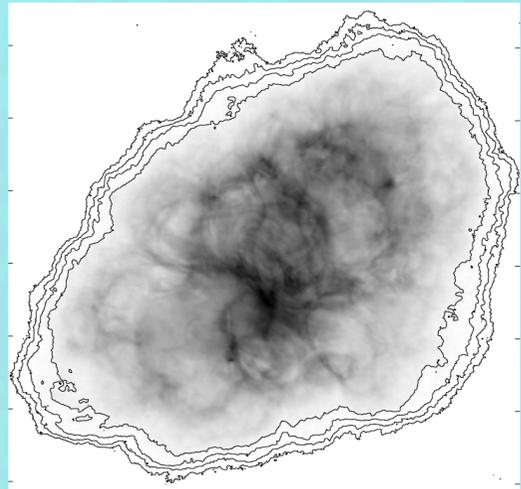
- mean **B-field** inside PWN.
- particle energy & number inside PWN.
- magnetization at injection.
- particle injection spectrum (broken PL).
- spin evolution of the central PSR.

# Virtue of

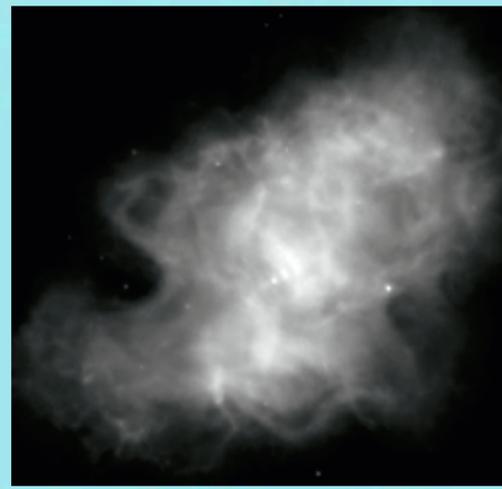
Bright and extended object

• Brightness map in different frequencies of the Crab.

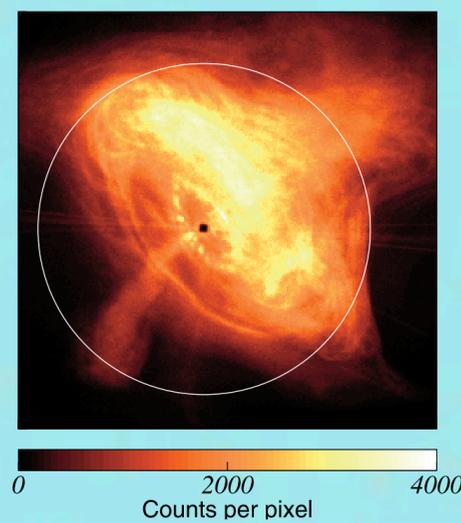
Bietenholz+04ApJ (radio)



Temim+06ApJ (IR)



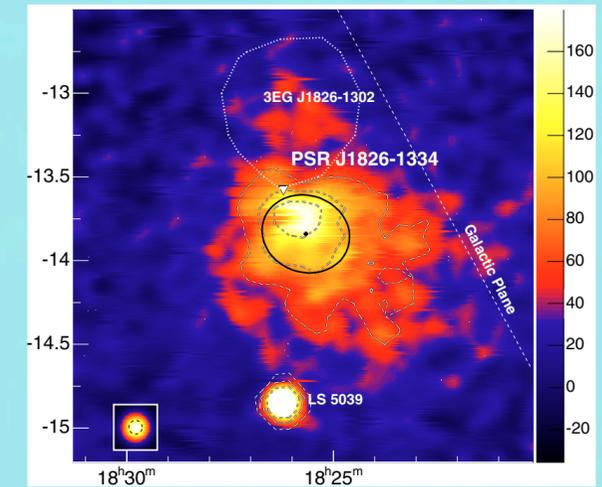
Mori+04ApJ (X-ray)



Crab は 点源なので



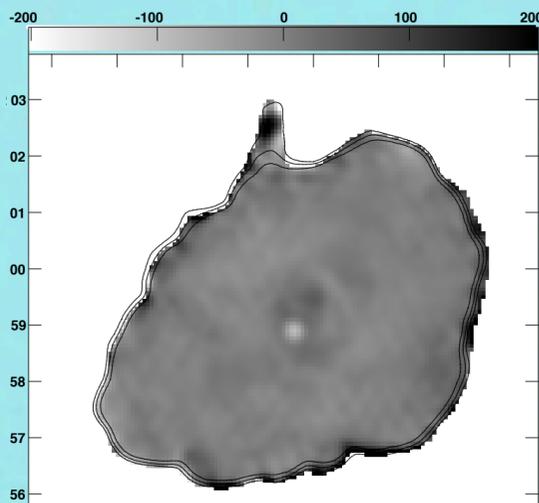
HESS J1825-137



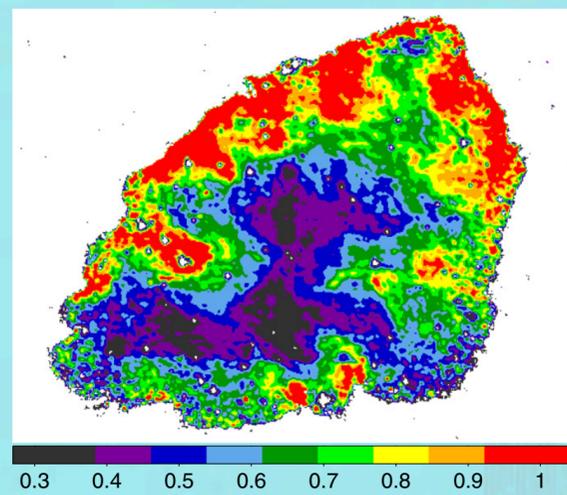
Aharonian+06A&A (γ-ray)

• Spectral index map in different frequencies of the Crab.

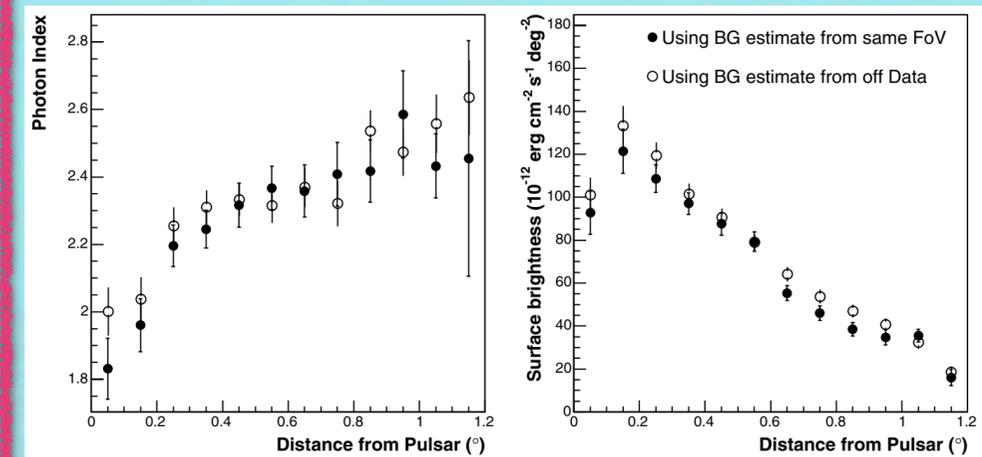
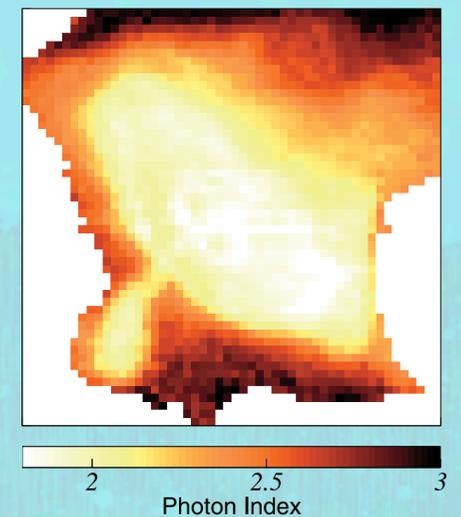
Bietenholz+97ApJ (radio)



Temim+12ApJ (IR)



Mori+04ApJ (X-ray)



PWN emission reflects B-field & particle distribution of PWN

# Motivation

What do we learn from observations of the Crab Nebula?

## PSR & PWN properties

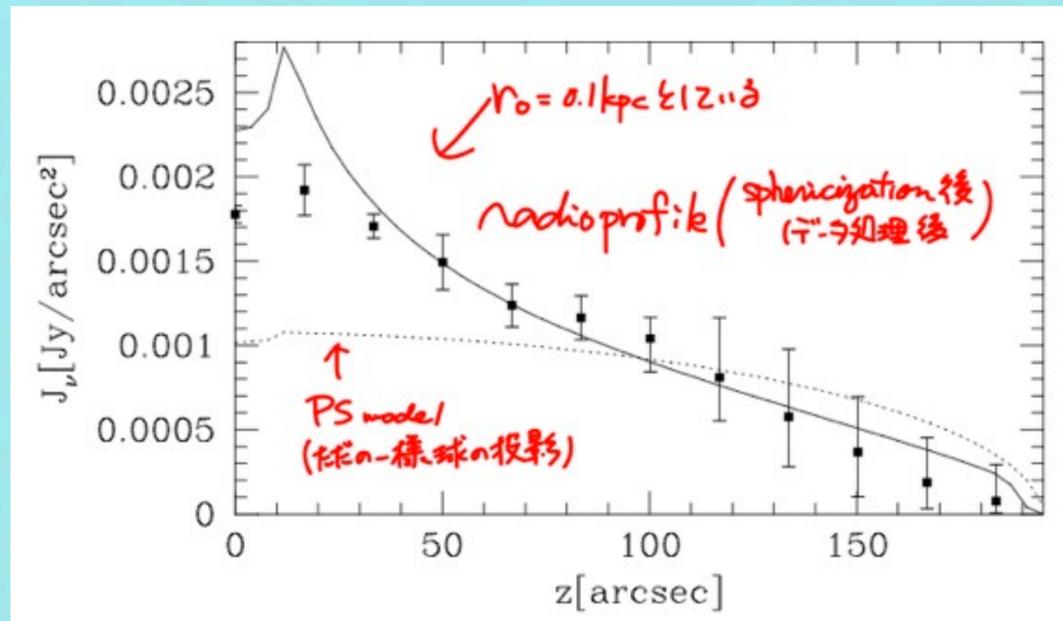
- Magnetization of pulsar wind. →  $\sigma$ -problem
- Injection spectrum of particles. →  $\kappa$ -problem & particle acceleration
- $e^\pm$  escaping process from PWN. → PAMELA anomaly

## Physics

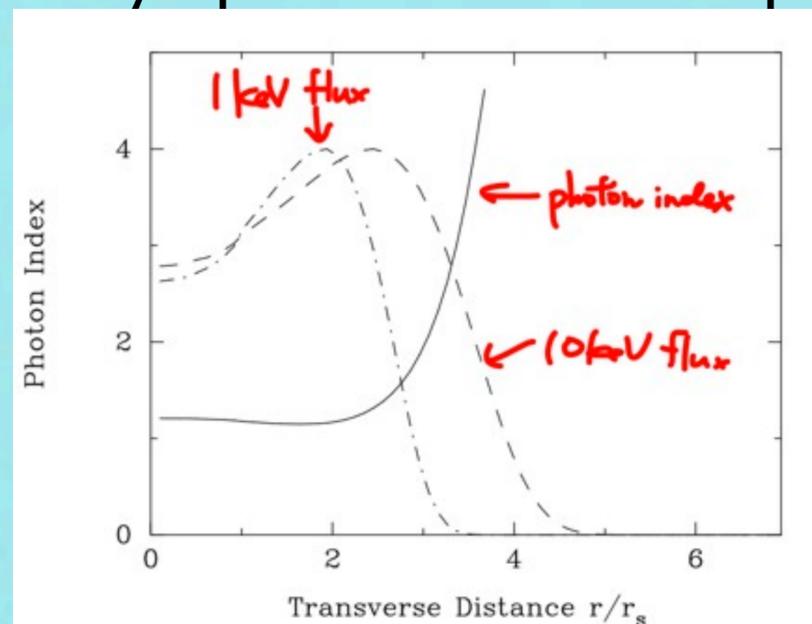
- Particle transport mechanism inside PWN. → advection? diffusion?
- Particle acceleration process inside PWN. → second-order acceleration?
- Expansion of PWN. → Interaction between PWN & SNR at outer boundary.

# Past Studies

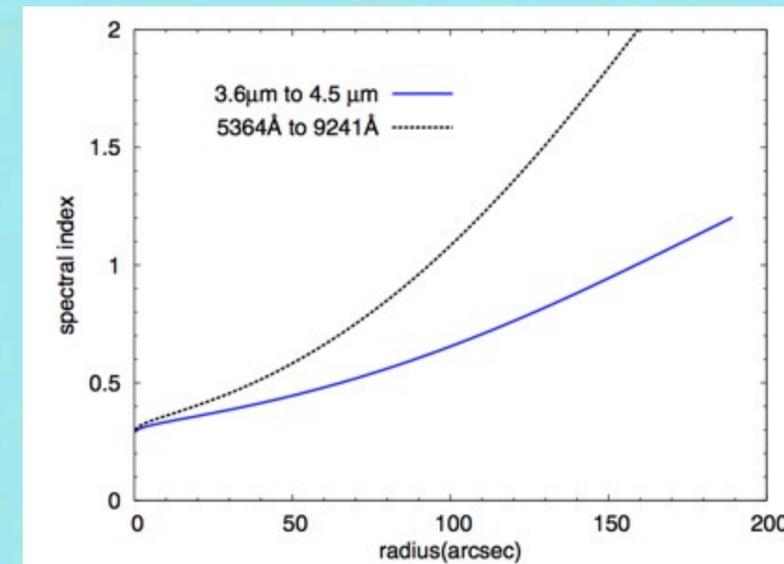
Amato+00, advection only  
Radio brightness map



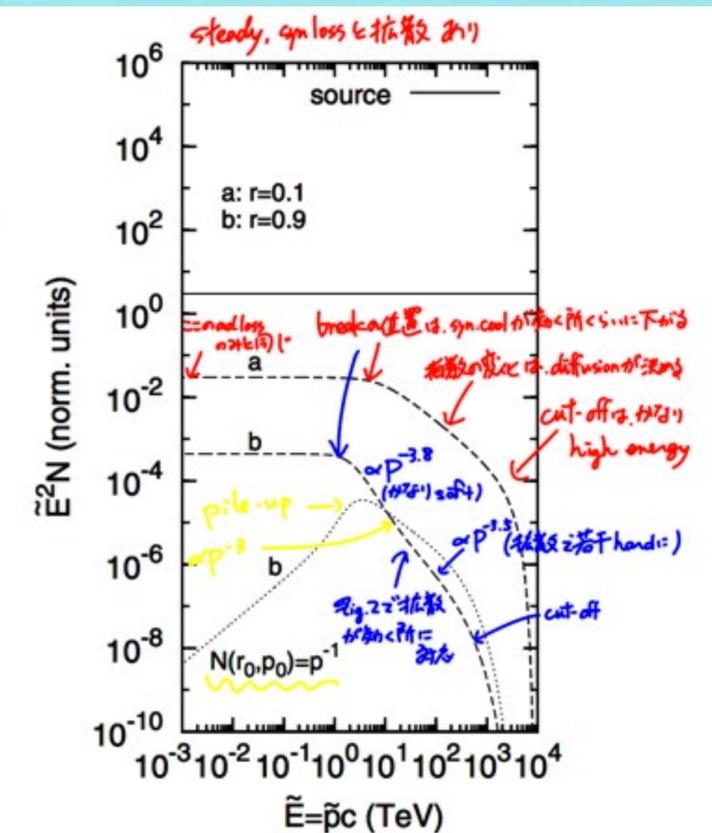
Reynolds03, advection only  
X-ray spectral index map



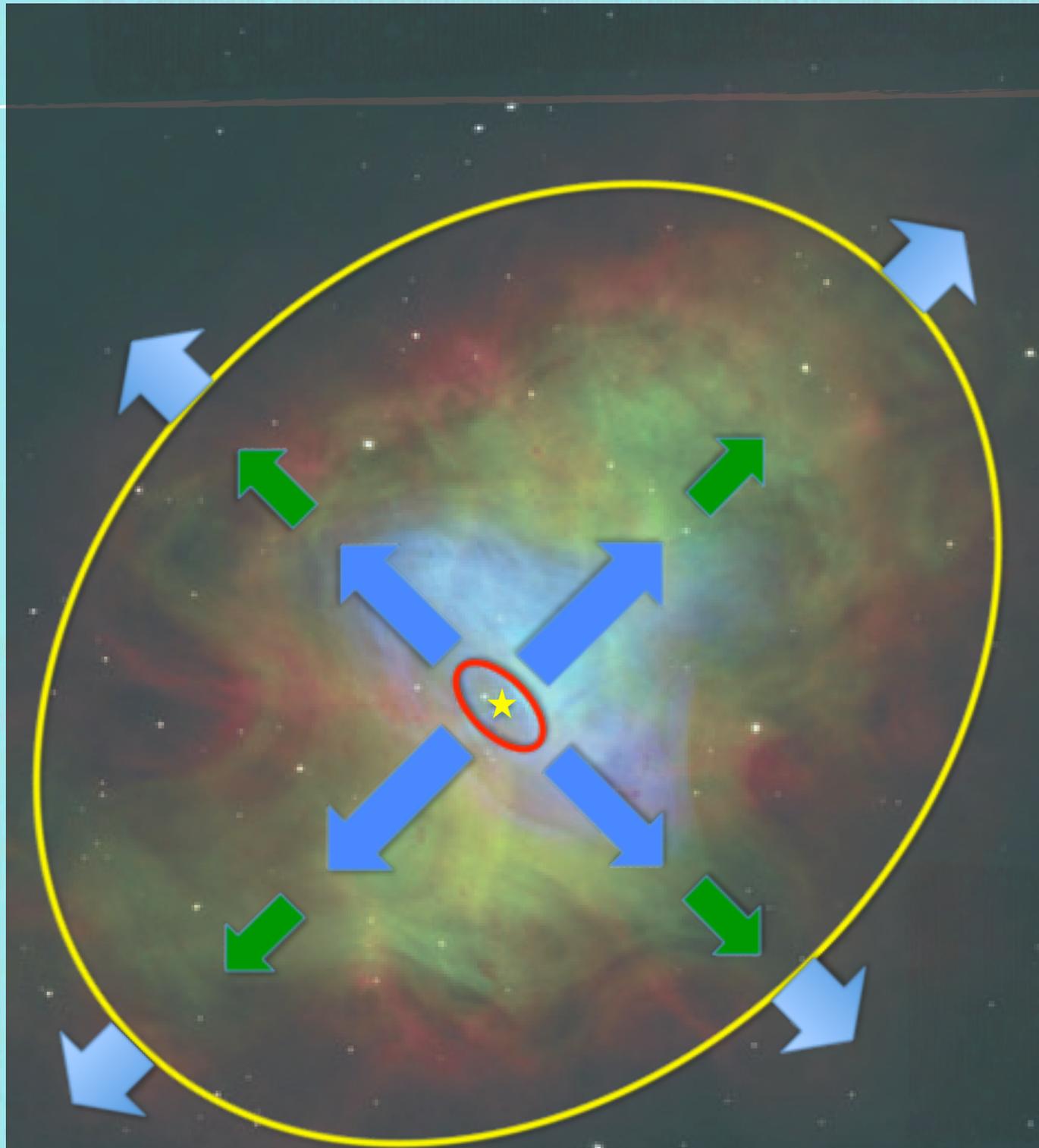
Tang & Chevalier12, diffusion  
optical spectral index map



Vorstar & Moraal13, diffusion & advection  
particle spectrum



# 1D - Model



## Dynamics

- radial expansion

$$\mathbf{v}(r) = v_0 \left( \frac{r}{r_0} \right)^{-\alpha_v} \mathbf{e}_r$$

- toroidal B-field

$$\mathbf{B}(r, t_{\text{inj}}) = B(t_{\text{inj}}) \left( \frac{r}{r_0} \right)^{-\alpha_B} \mathbf{e}_\varphi$$

- induction equation (MHD condition)

$$\frac{\partial \mathbf{B}}{\partial t} = \nabla \times (\mathbf{v} \times \mathbf{B})$$

- parameters

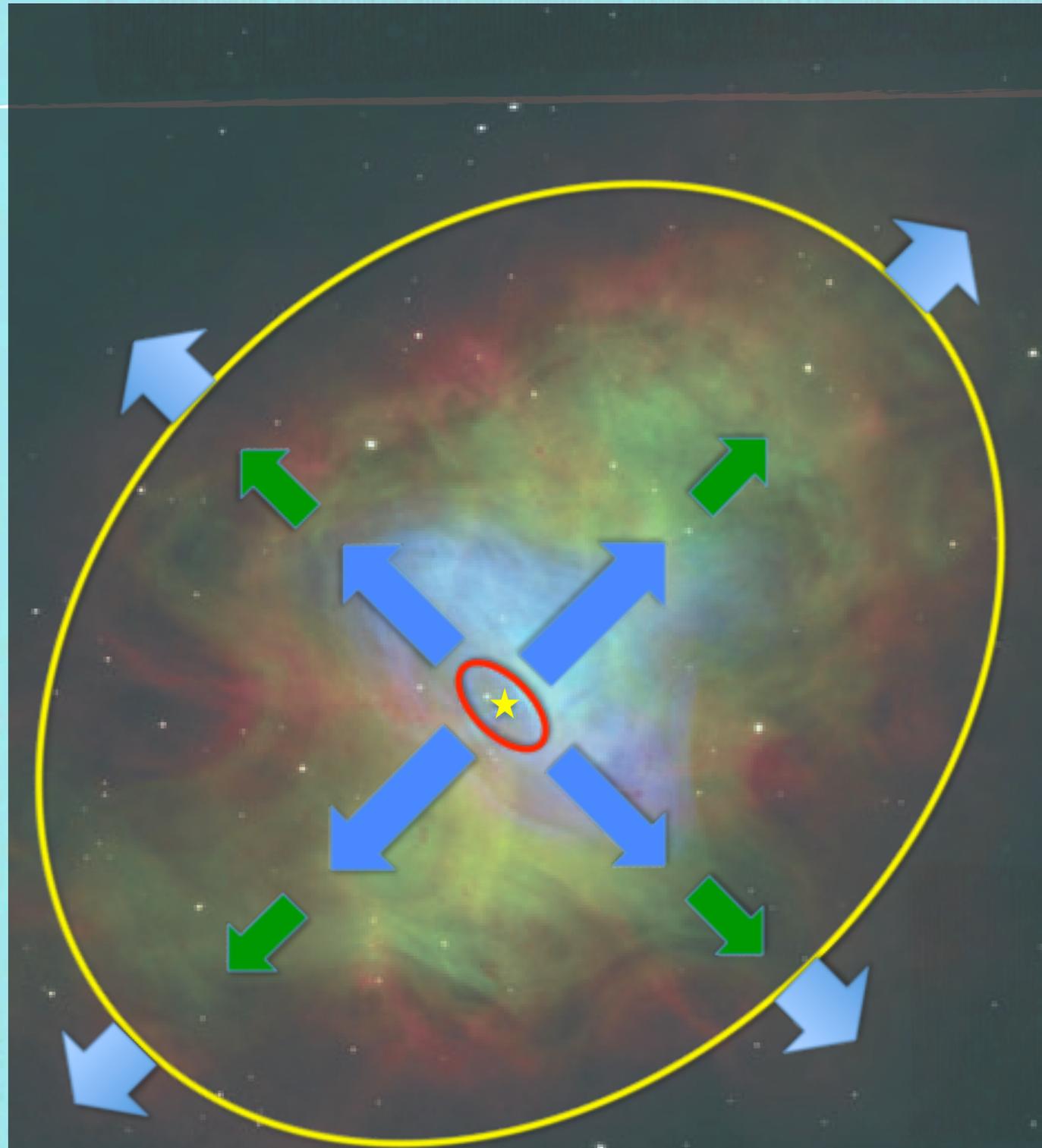
inner radius:  $r_0$

inner velocity:  $v_0$

vel. profile index:  $\alpha_v$

injection B-field:  $B_{\text{inj}}$

# 1D - Model



## Particle Spectrum

- **diffusion & convection transport**

**+ adiabatic & radiative cooling**

$$\frac{\partial f}{\partial t} = -\nabla \cdot [(\mathbf{v} - K\nabla)f] + \frac{1}{p^2} \frac{\partial}{\partial p} \left[ \left( \frac{1}{3} \nabla \cdot \mathbf{v} + (\beta_{\text{syn}} + \beta_{\text{IC}}) p^3 f \right) p^3 \right] + Q_{\text{inj}}$$

- **diffusion coefficient**

$$K = \frac{1}{3} \xi c r_{\text{gyro}}$$

- **injection spectrum**

$$Q_{\text{inj}}(r, t, p) = q(t) \frac{\delta(r - r_0)}{4\pi r_0^2} \times \begin{cases} (p/p_b)^{2-p_1} & \text{for } p_{\text{min}} \leq p \leq p_b, \\ (p/p_b)^{2-p_2} & \text{for } p_b \leq p \leq p_{\text{max}}, \end{cases}$$

- **parameters**

**diffusion coefficient:  $\xi$**

**injection parameters:  $p_1, p_2, \gamma_{\text{min}}, \gamma_{\text{max}}, \gamma_b$**

# Mimicking the Crab Nebula

We consider that the particles and the magnetic field are injected at the inner radius  $r = r_0$  at a time  $t = t_{inj}$ .

Main parameters are

1. gyro-factor  $\xi$ ,

2. inner radius  $r_0$  or velocity profile index  $\alpha_v$ ,

$$R_{PWN} = 2.0\text{pc}, V_{PWN} = 1.500\text{km/s @ } t_{age} = 1\text{kyr}$$

( $r_0 = 0.1\text{pc}$  &  $v_0 = c/3$  are too much.)

3. injected B-field or magnetization  $\sigma$

$$B_0 = 300\mu\text{G}$$

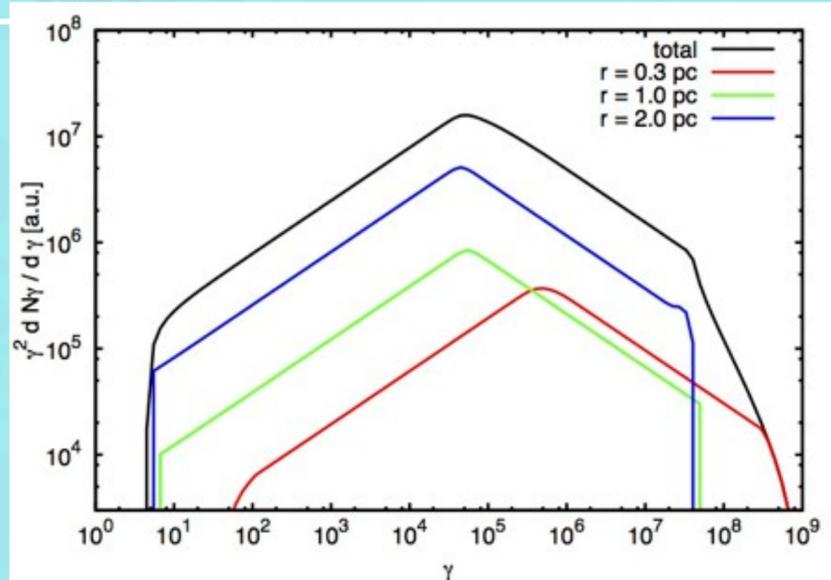
4. broken power-law injection with

$$p_1 = 1.5, p_2 = 2.5, \gamma_{min} = 10^2, \gamma = 10^6, \gamma_{max} = 10^9$$

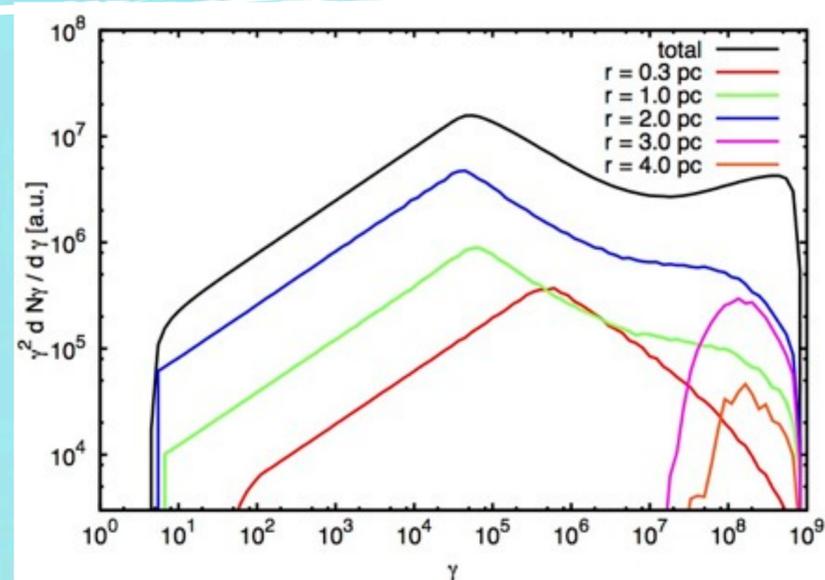
# Results: Particle

$r_0 = 0.007 \text{ pc}$

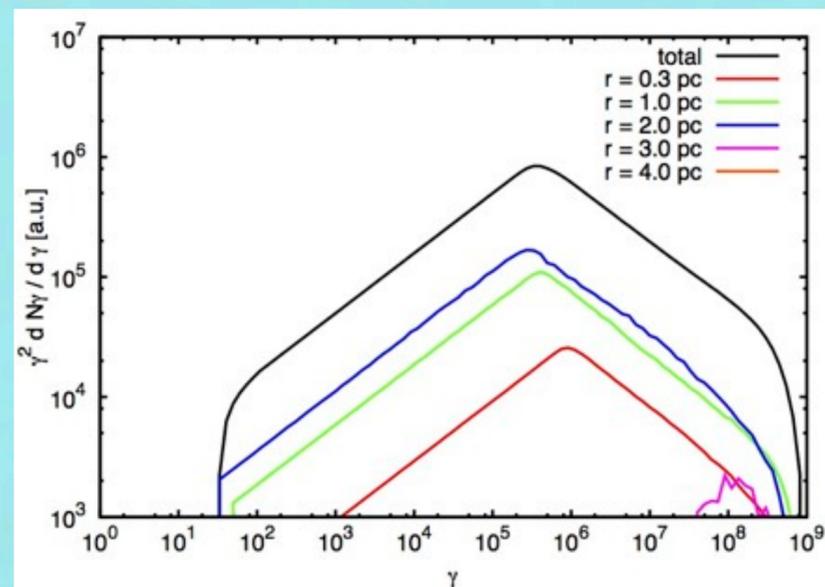
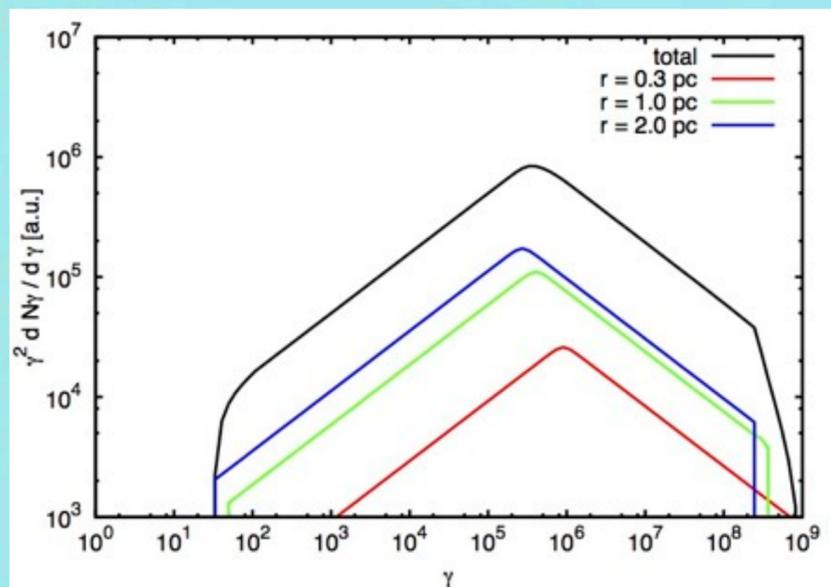
without diffusion



with diffusion( $\xi=1$ )



$\propto e$



1. strong adiabatic cooling for  $r_0 = 0.007 \text{ pc}$ .

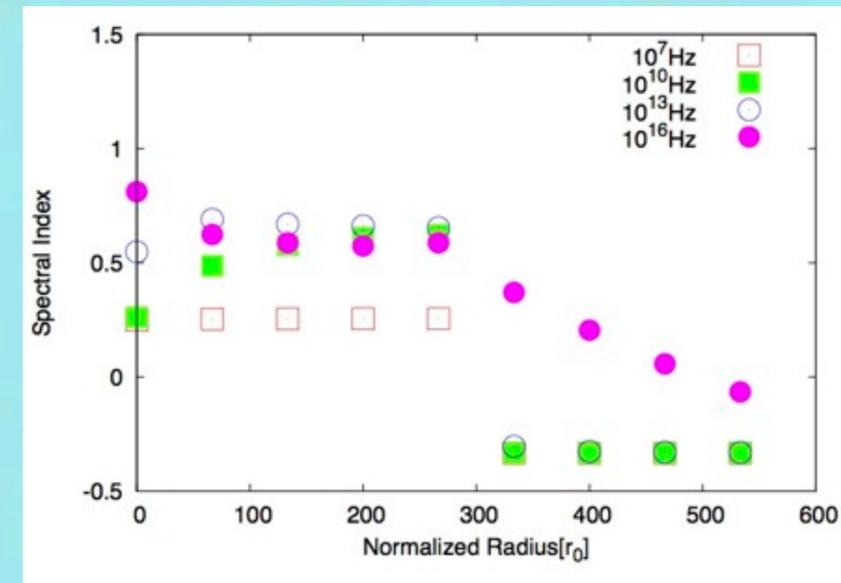
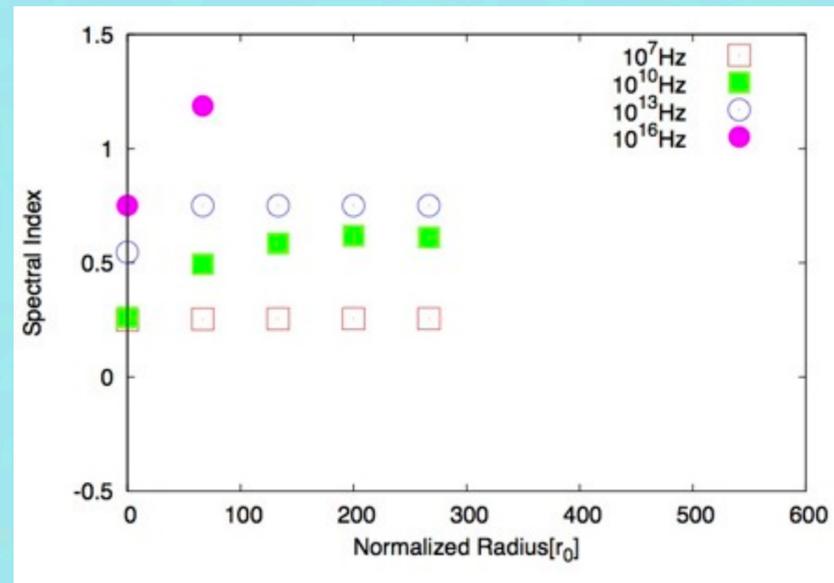
2. When  $\xi$  is non-zero,  $e^\pm$  can escape from PWN ( $r \gg R_{\text{PWN}}$ ).

3. Escaped high energy  $e^\pm$  are cooled slowly.

4. For  $r_0 = 0.007 \text{ pc}$ , because  $r_0$  is smaller than diffusion length for high energy  $e^\pm$ , more particles can escape than for  $r_0 = 0.2 \text{ pc}$ , mostly in an early phase of evolution.

# Results: Spectral Index Profile

$[r_0 = 0.007\text{pc, i.e., } R_{\text{PWN}} \sim 300r_0]$



$p_1 = 1.5$  &  $p_2 = 2.5$  corresponds  $\alpha = 0.25$  &  $0.75$

1. Without diffusion, we find synchrotron cooling effect increases spectral index at  $10^{16}\text{Hz} > 10$  at  $100r_0 \sim 0.7\text{pc}$ .
2. Diffusion effect smooths spectral index profile and we do not find synchrotron cooling hardening of the spectrum for  $B_0 = 100\mu\text{G}$ . We need to select appropriate parameter set of  $(\xi, B_0)$  to fit the spectral index distribution.
3.  $\alpha = -1/3$  corresponds to low freq. side of synchrotron spectra and is appeared at  $r > R_{\text{PWN}} @ < 10^{16}\text{Hz}$ .

# Conclusion

- Convection–Diffusion transport equation is considered to study the broadband emission structure of PWNe.
- For the escaping of  $e^\pm$  from PWNe, we should compare diffusion length &  $r_0$ .
- $\gamma$ -ray distribution almost traces the particle distribution for inverse Compton scattering off CMB.
- Synchrotron Self–Compton process is considered to be dominated in the Crab Nebula in  $\gamma$ -rays and should be considered the future work.
- We need larger value of B-field at injection point, to obtain softer spectra observed for many PWNe in X-rays ( $\alpha > 2$ ).